



EDMI Microsystems and Microelectronics

MICRO-614: Electrochemical Nano-Bio-Sensing
and Bio/CMOS interfaces

Lecture #3

Probe/Target interactions (DNA/Antibodies/Enzymes)

Lecture Outline

(Book Bio/CMOS: Chapter' paragraphs § 4.4-16)

- DNA/RNA pairing & Bond energy
- Antibody/Antigen affinity & Bond energy
- Enzymes/substrates & Reaction Energy
- Atypical Enzymatic Kinetics

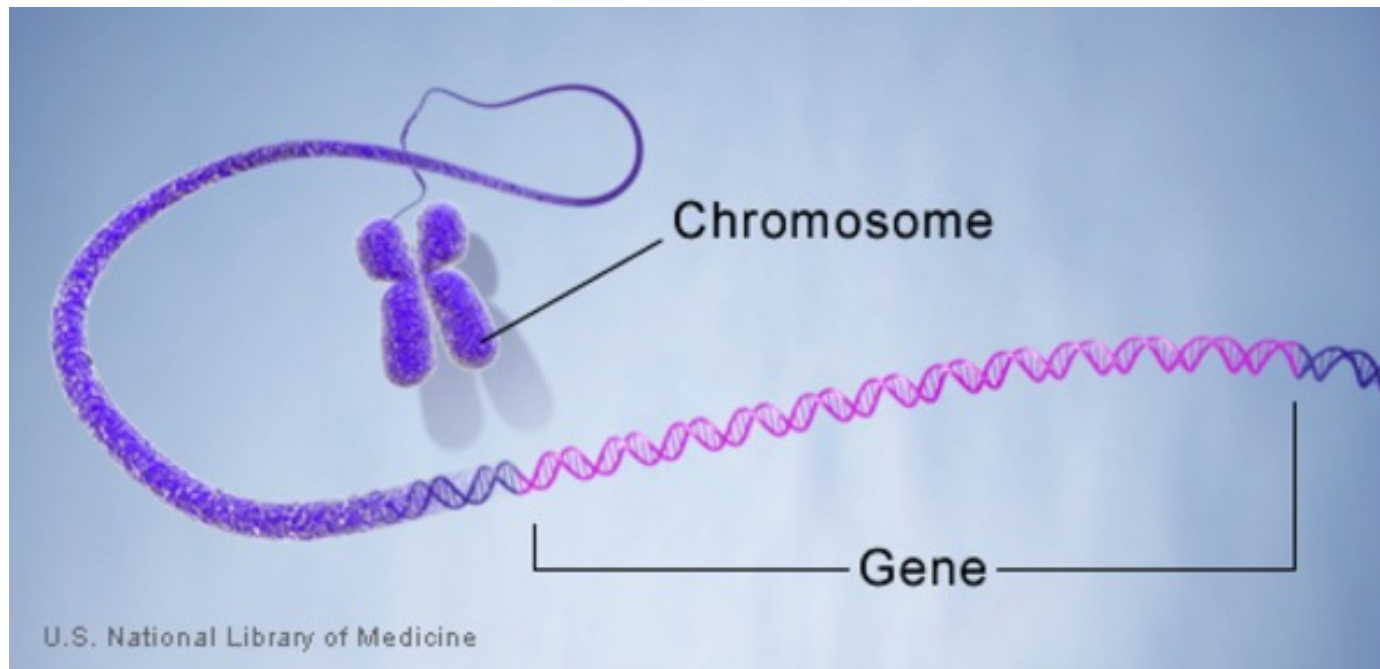
DNA



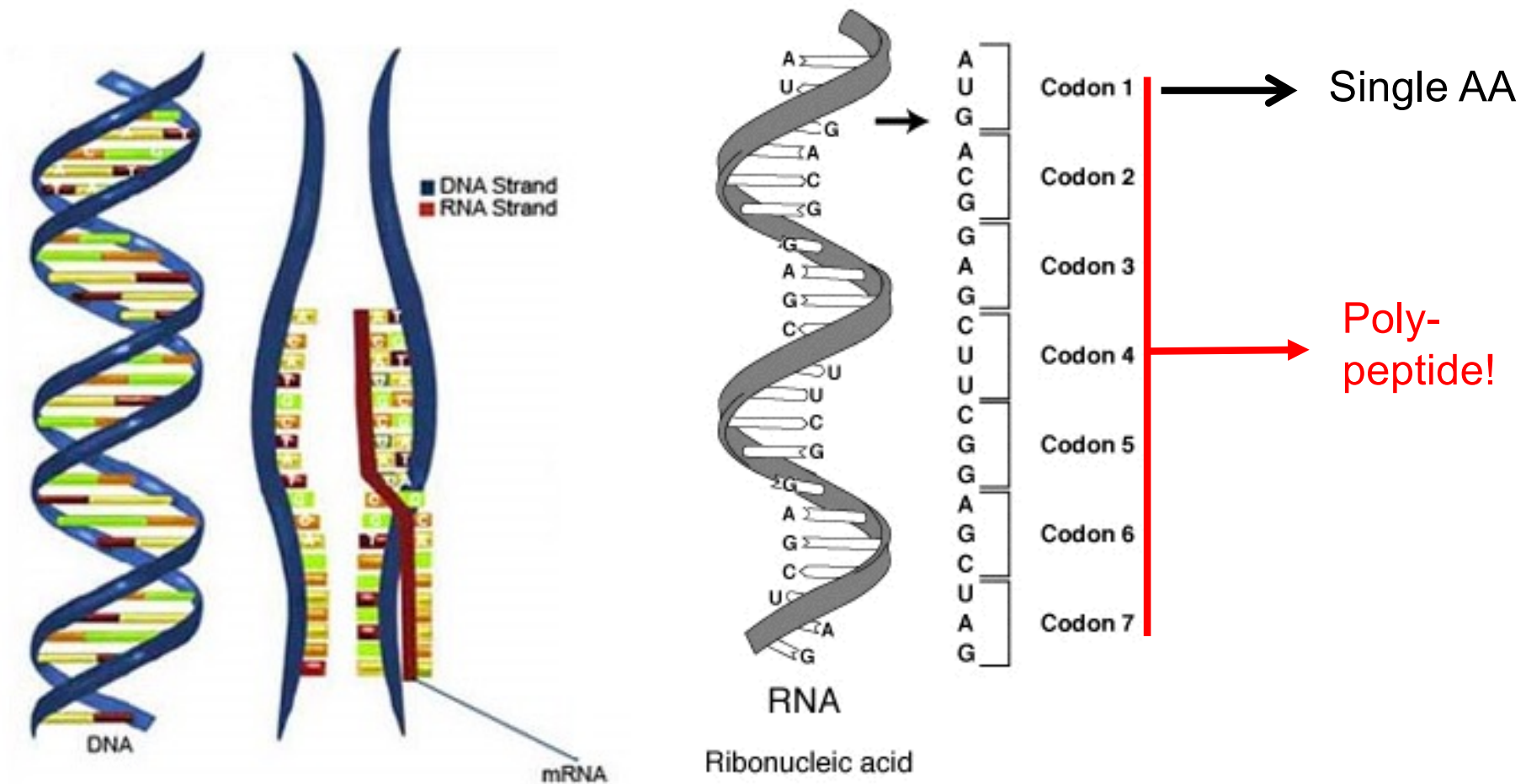
Another fundamental molecules in
Biochemistry is the DNA

DNA codes the genes

The function of DNA is to store all of the genetic information that organisms need to develop and self-reproduce

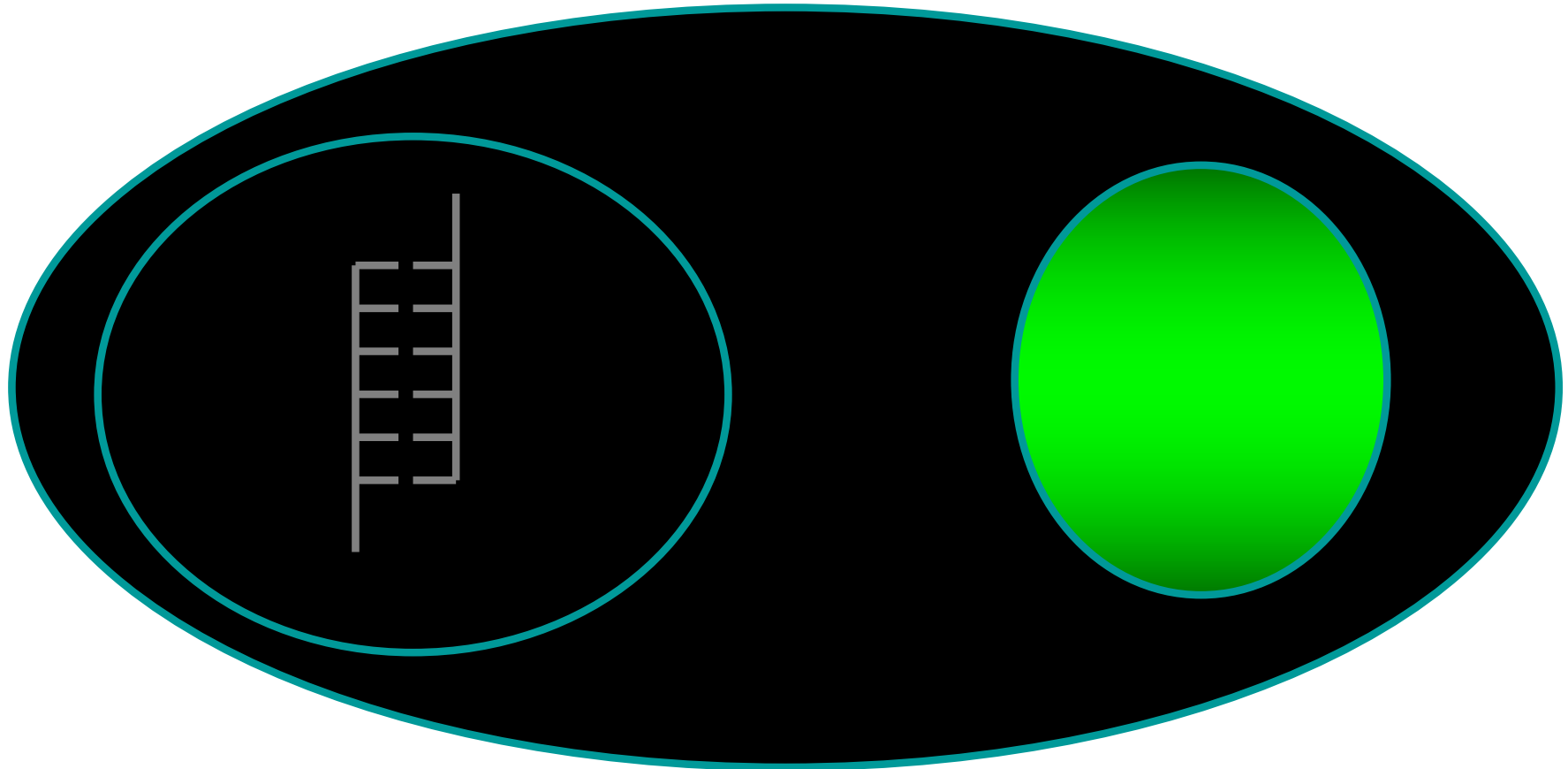


RNA decodes the genes



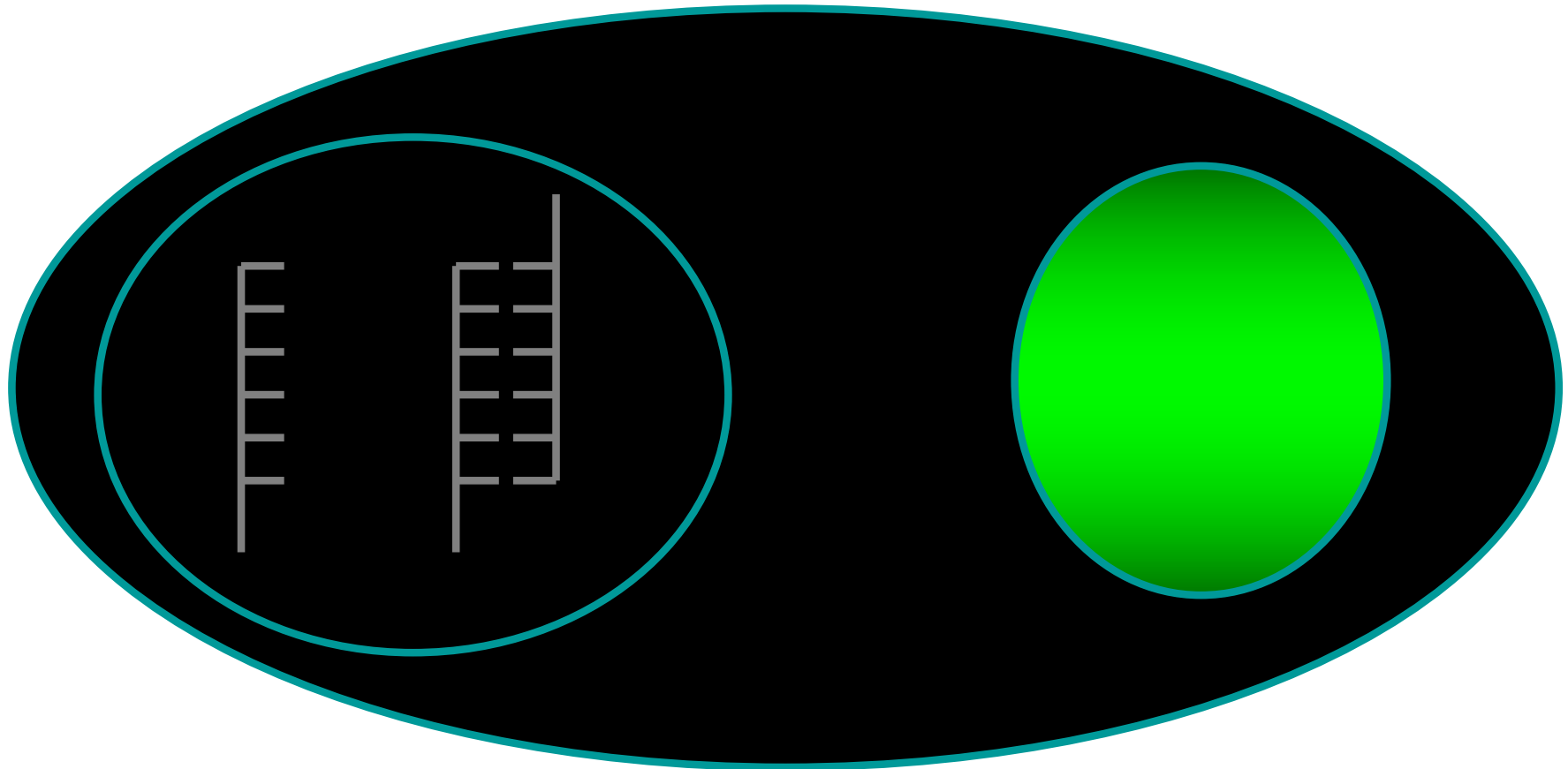
The RNA is another similar molecule useful to decode the genetic code

DNA/RNA functions in cells



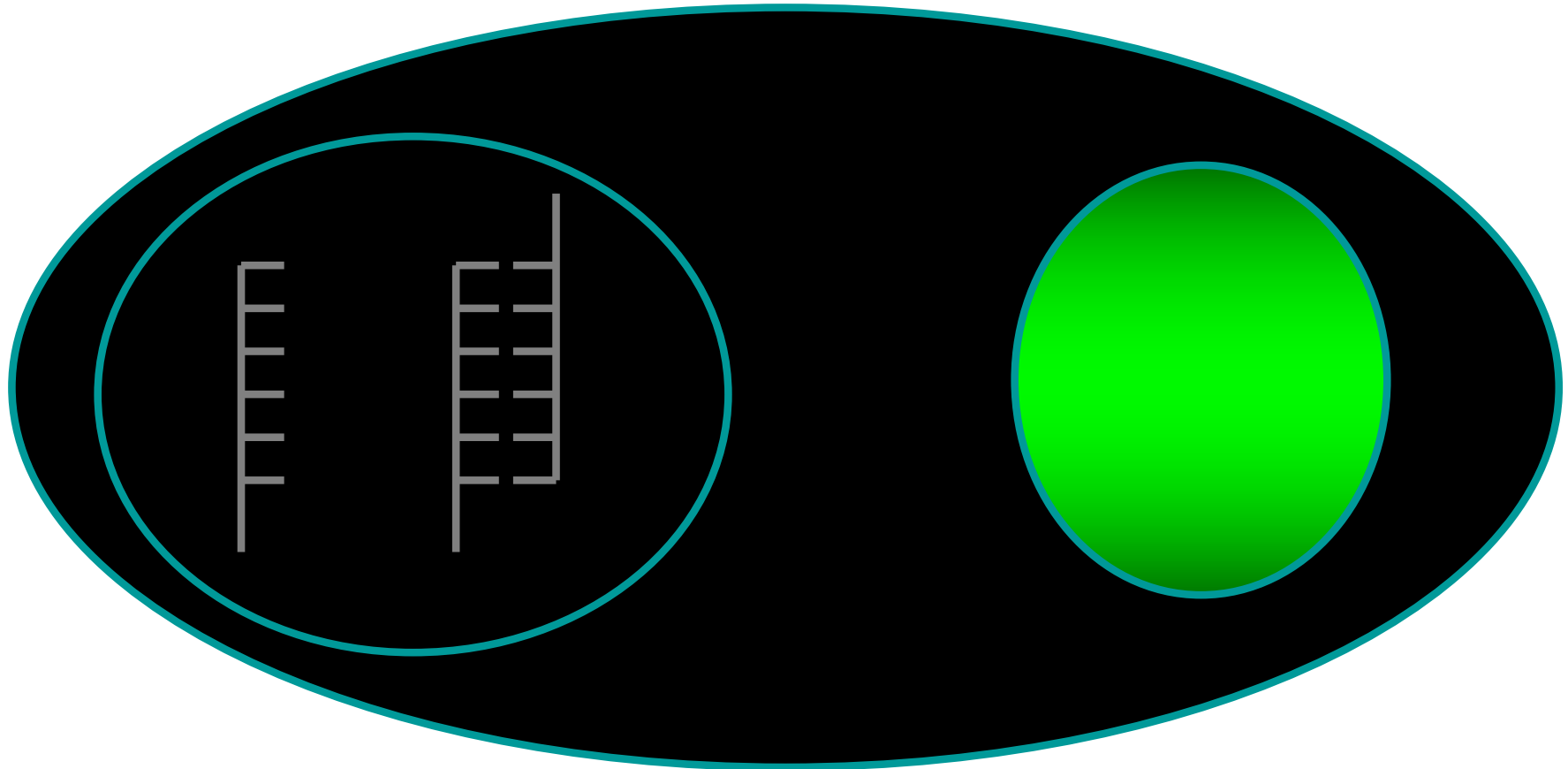
The DNA double helix is opened

DNA/RNA functions in cells



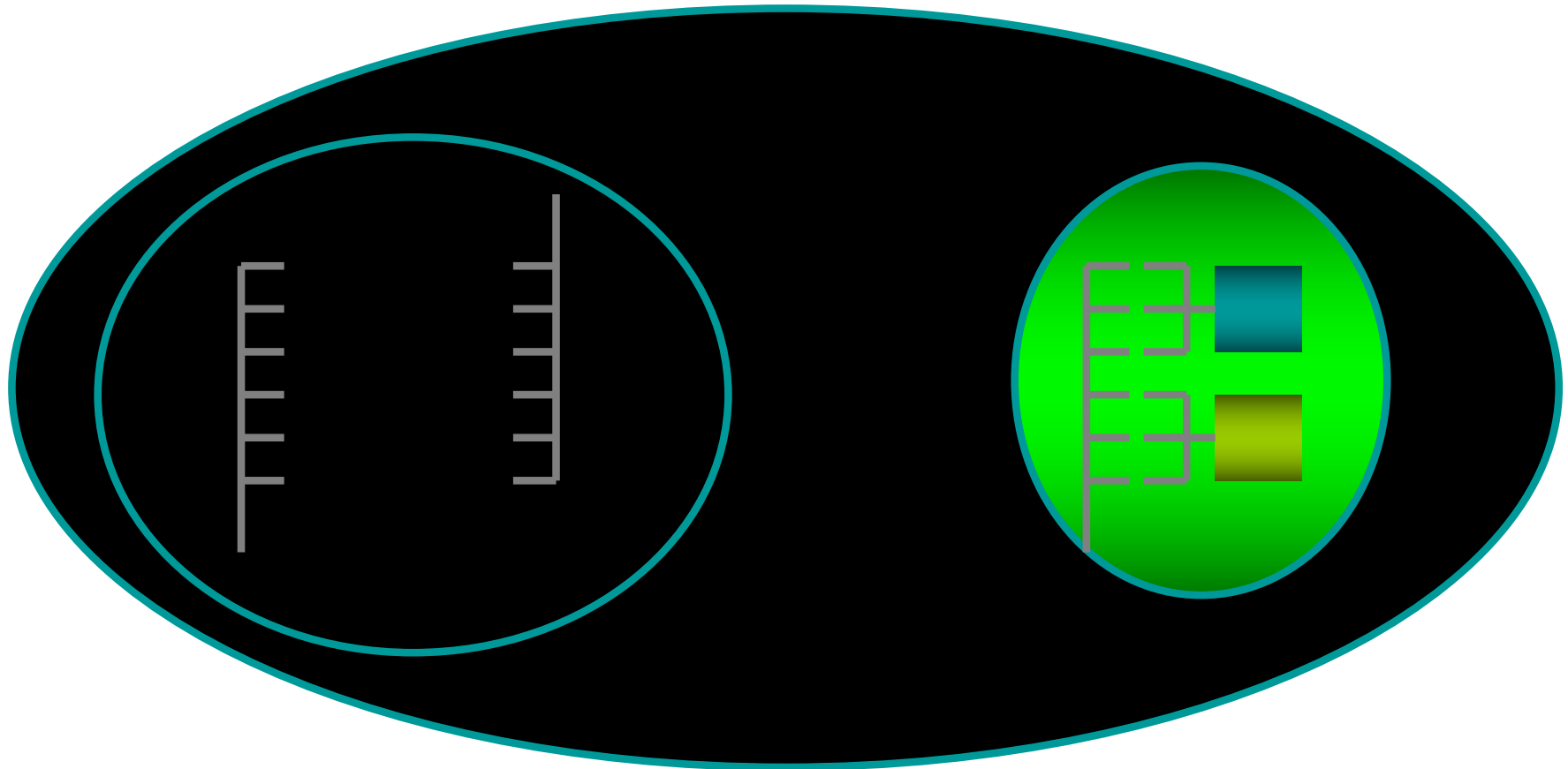
The genetic encoded in DNA is replicated in the messenger RNA molecule

DNA/RNA functions in cells



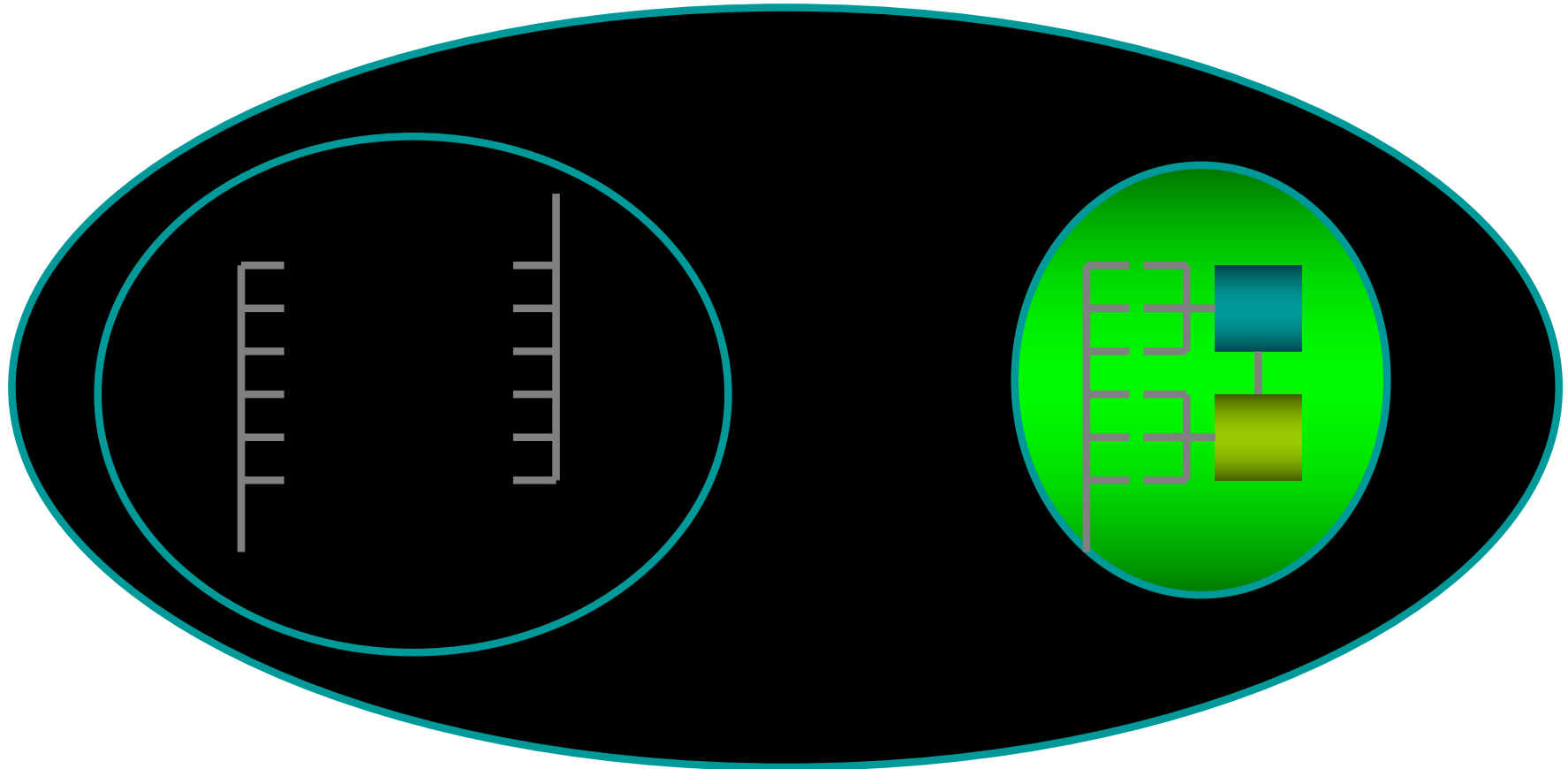
The mRNA is transferred into the ribosome

DNA/RNA functions in cells



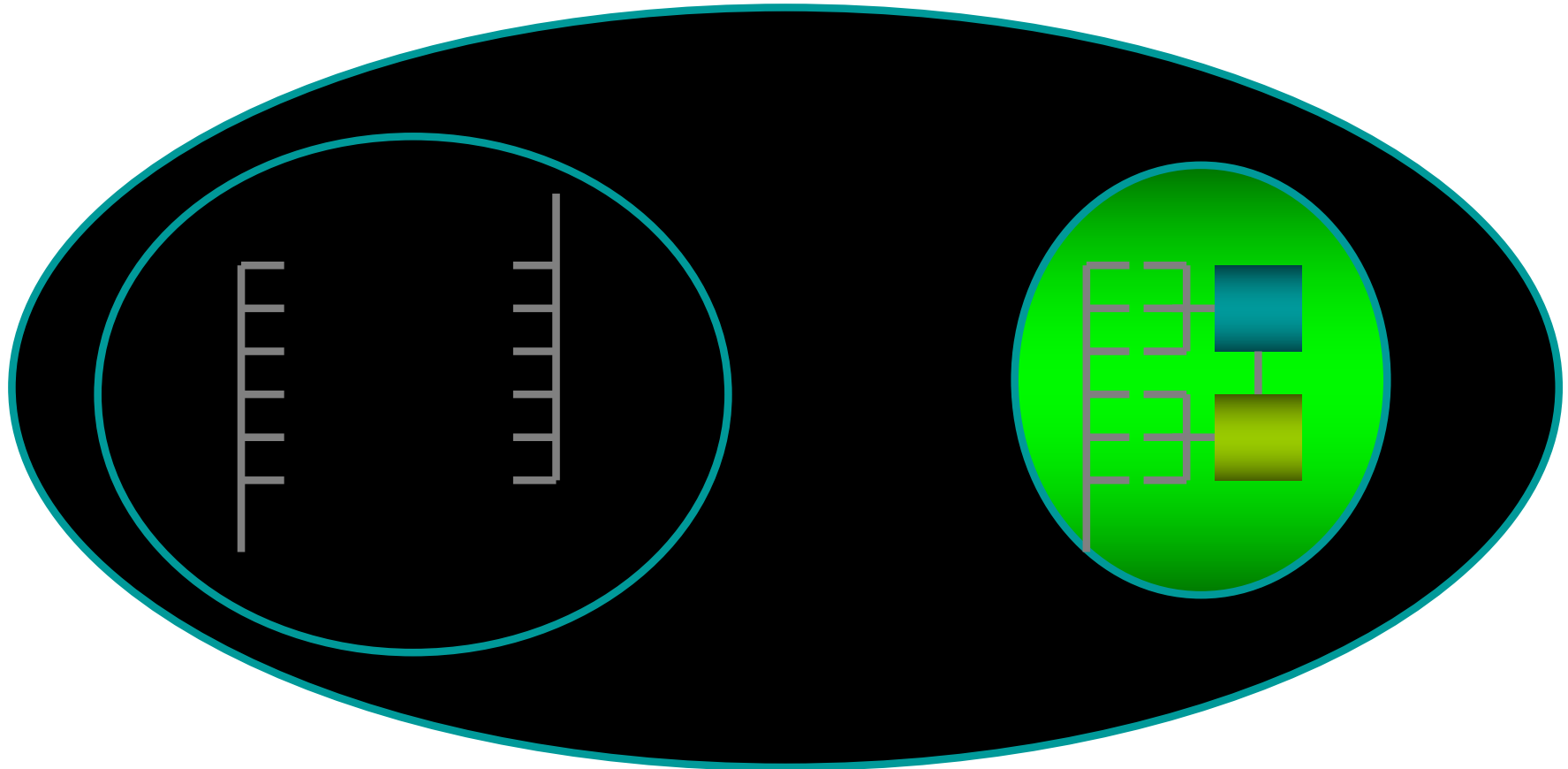
In the Ribosome, the transfer-RNA decode in polypeptides the genetic code carried by mRNA

DNA/RNA functions in cells



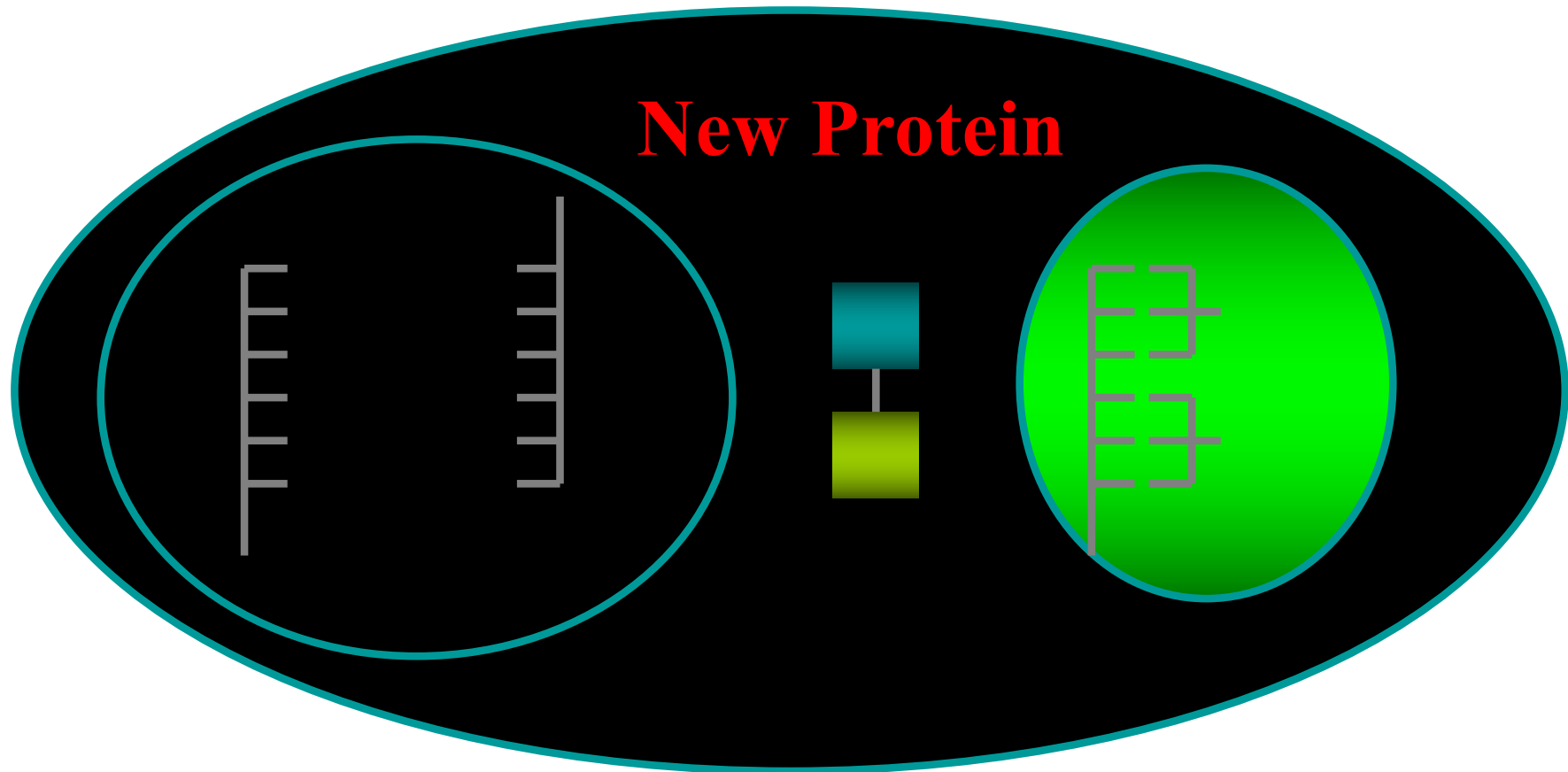
The poly-peptides form new proteins

DNA/RNA functions in cells



New proteins are, then, released
into the cell cytoplasm

RNA function in the cell

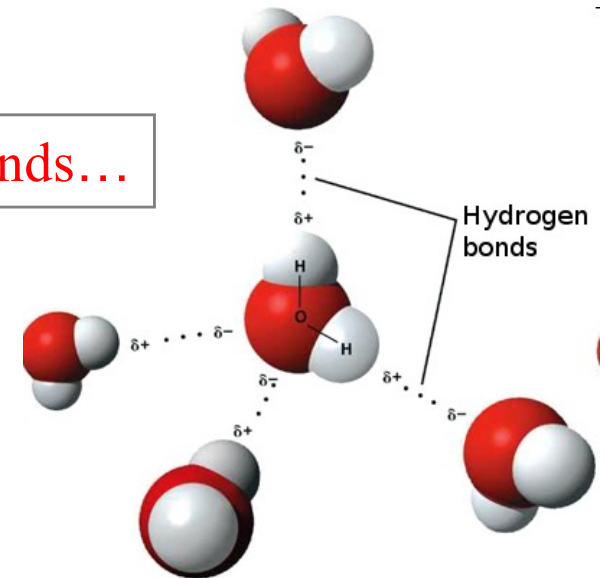


New proteins into the cell cytoplasm
enable the cell metabolism

DNA Base pairing

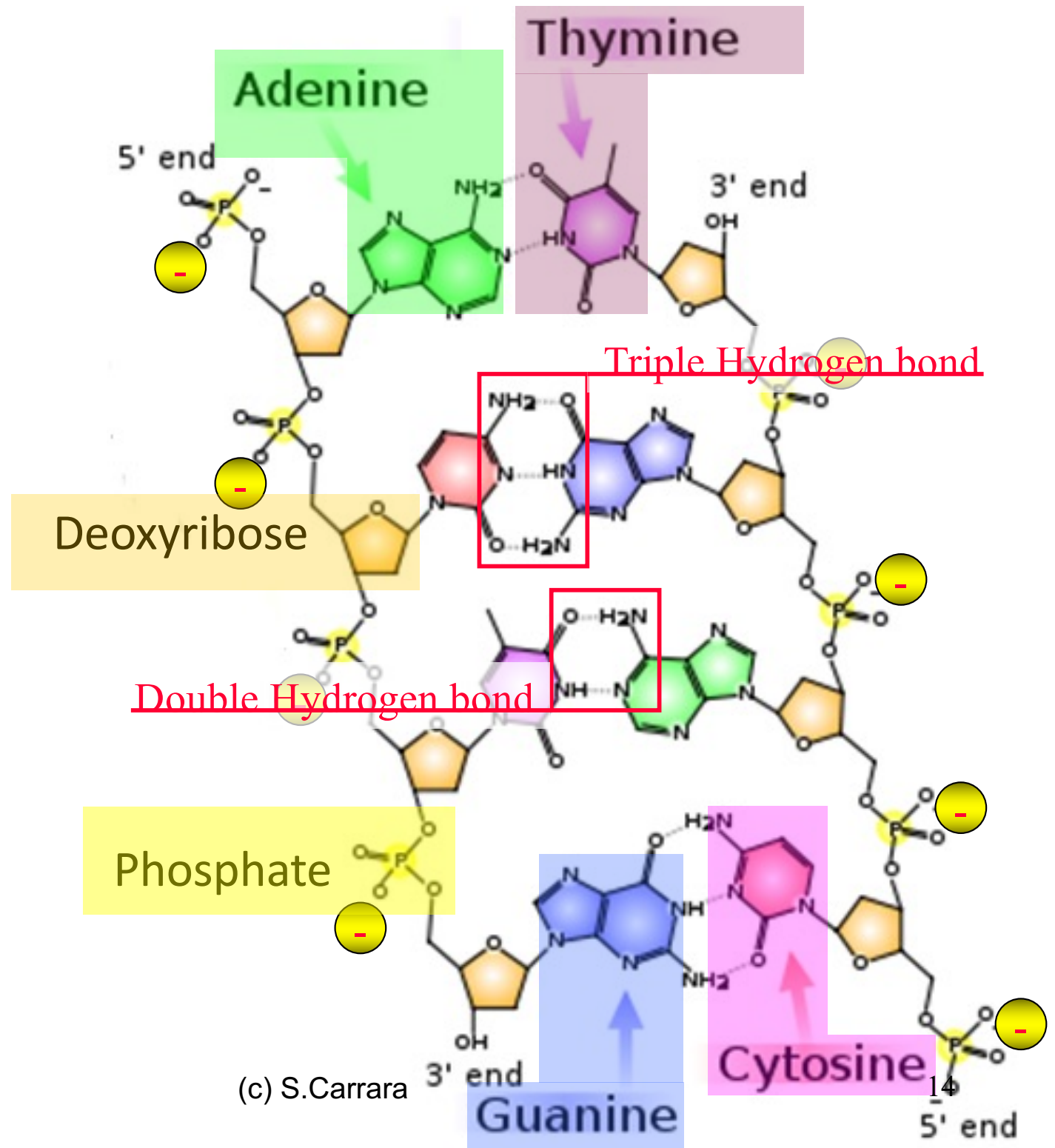
Each type of base on one strand forms a bond with just one type of base on the other strand. This is called **complementary base pairing**.

Thanks to Hydrogen Bonds...

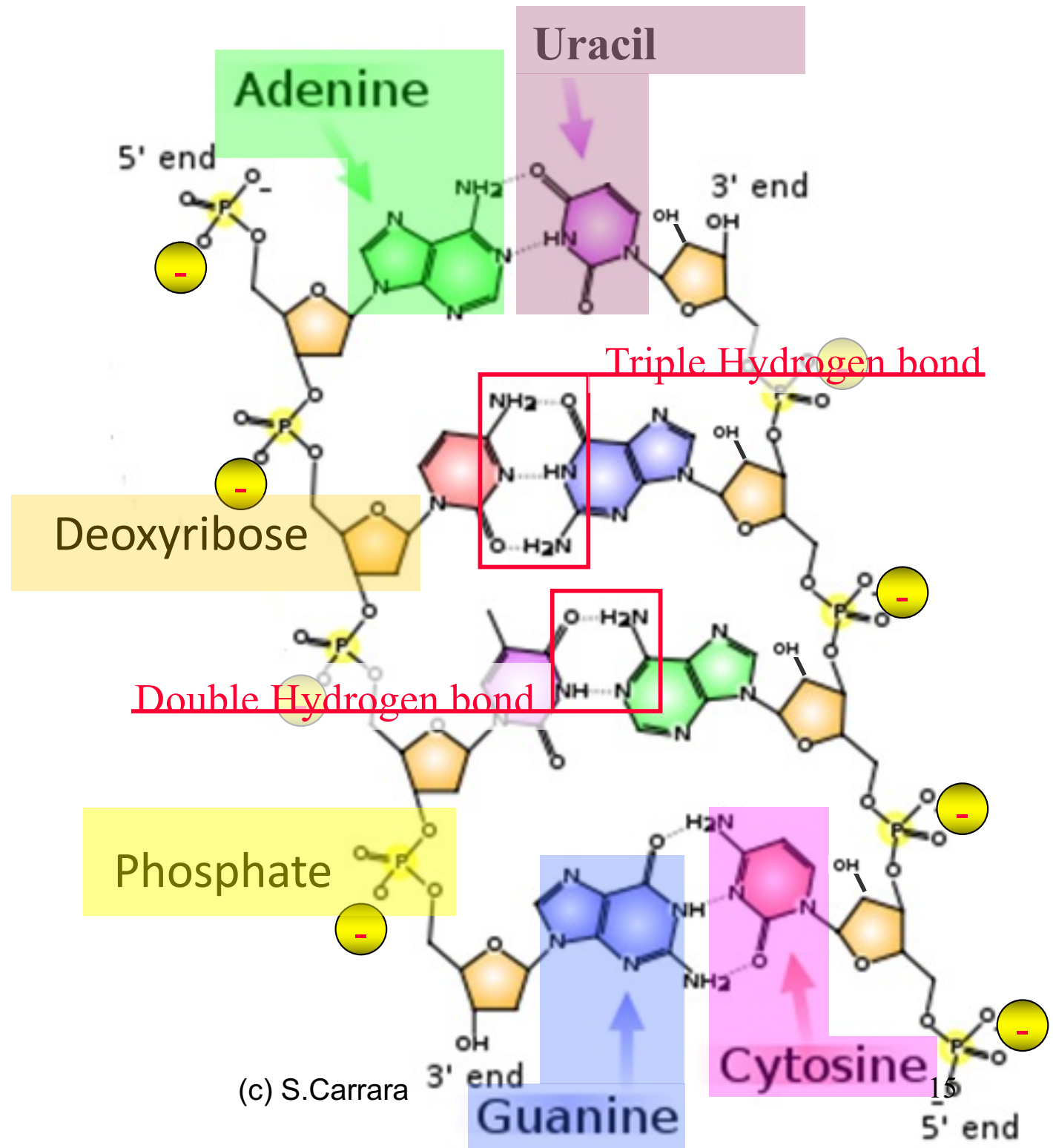


(c) S.Carrara

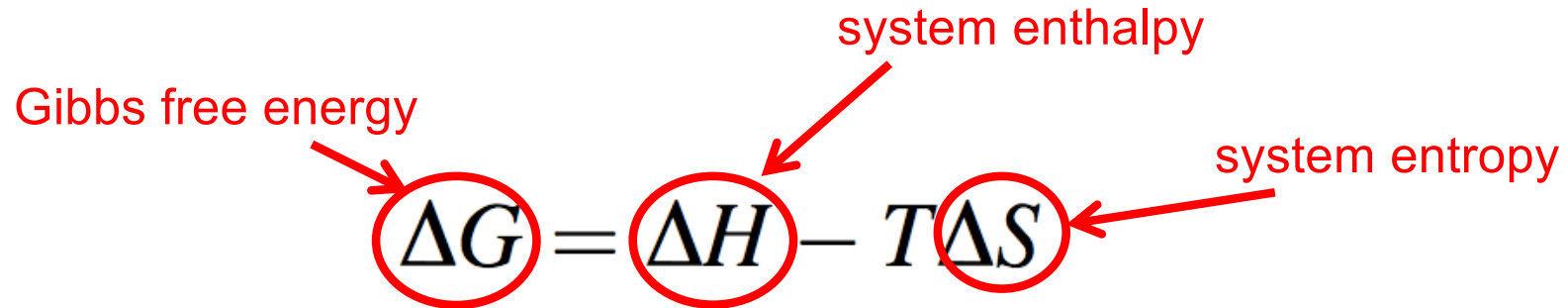
DNA-DNA Interaction



DNA-RNA Interaction



Gibbs free energy



The diagram shows the equation $\Delta G = \Delta H - T\Delta S$. Three red circles are drawn around the terms ΔG , ΔH , and $T\Delta S$. Red arrows point from text labels to these circles: 'Gibbs free energy' points to ΔG , 'system enthalpy' points to ΔH , and 'system entropy' points to $T\Delta S$.

$$\Delta G = \Delta H - T\Delta S$$

The Gibb free energy is the upper limit (some times called thermodynamic potential) of the total work obtainable by the system in processes at constant temperature and pressure

The enthalpy is related to variations in **stacking energy** related to bond strength, which includes but is not limited to **hydrogen bonds** strength

The entropy is kind of measure of the system disorder and $T\Delta S$ is the energy generated/adsorbed by the system in the conformational change

Enthalpy & entropy for different DNA dimers

DNA dimer	ΔH [kJ/mol]	ΔS [kJ/(mol K)]
$\begin{array}{c} 5' \uparrow \text{A-T} \beta' \\ \\ 3' \downarrow \text{T-A} \downarrow 5' \end{array}$	-30.2	-85.4
$\begin{array}{c} \uparrow \text{A-T} \\ \text{A-T} \downarrow \end{array} \text{ or } \begin{array}{c} \uparrow \text{T-A} \\ \text{T-A} \downarrow \end{array}$	-33.1	-92.9
$\begin{array}{c} \uparrow \text{T-A} \\ \text{A-T} \downarrow \end{array}$	-30.2	-89.2
$\begin{array}{c} \uparrow \text{G-C} \\ \text{C-G} \downarrow \end{array}$	-41.0	-102.1
$\begin{array}{c} \uparrow \text{G-C} \\ \text{G-C} \downarrow \end{array} \text{ or } \begin{array}{c} \uparrow \text{C-G} \\ \text{C-G} \downarrow \end{array}$	-33.5	-83.3
$\begin{array}{c} \uparrow \text{C-G} \\ \text{G-C} \downarrow \end{array}$	-41.9	-113.9

Enthalpy & entropy for different DNA dimers

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$\begin{array}{c} \uparrow \text{C-G} \downarrow \\ \text{G-C} \end{array}$	-41.9	-113.9

So, Sequence matters in the interaction strenght!

The Nearest-Neighbor Model

number of occurrences of each nearest neighbor

account for the initial pair

$$\Delta G = \sum_{\forall i} n_i \Delta G_i + \Delta G_i|_{init\ term\ A-T} + \Delta G_i|_{init\ term\ G-C} + \Delta G_{system}$$

Gibbs free energy change for the considered neighboring pairs

empirical parameter (+1.80 kJ/mol if the nucleic acid duplex is self-complementary, or equal to zero if not)

It introduces a computation for the total Gibbs free energy that takes into account the interactions from neighbours

Role of Solvent

$$\Delta G = \Delta G_{\text{double strand}}^{\text{intramol}} + \Delta G_{\text{double strand}}^{\text{solvent}} + \Delta G_{\text{single strand}}^{\text{solvent}}$$

solvation free energy of the double helix

intermolecular nucleic double strand acid interactions

solvation free energy of the single strands

The diagram shows the equation $\Delta G = \Delta G_{\text{double strand}}^{\text{intramol}} + \Delta G_{\text{double strand}}^{\text{solvent}} + \Delta G_{\text{single strand}}^{\text{solvent}}$. Three terms are circled in red. Red arrows point from descriptive text to each term: 'intermolecular nucleic double strand acid interactions' points to the first term, 'solvation free energy of the double helix' points to the second term, and 'solvation free energy of the single strands' points to the third term.

The solvent also plays a role in DNA/DNA and DNA/RNA pairing, thus, it contributes to the Gibbs free energy too

Role of Solvent

$$\Delta G = \Delta G_{double\ strand}^{intramol} + \Delta G_{double\ strand}^{solvent} + \Delta G_{single\ strand}^{solvent}$$

DNA/RNA hydrogen bonds interactions

$$\Delta G_{double\ strand}^{intramol} = \Delta G_{DNA-RNA}^{hydrogen\ bonds} + \Delta G_{DNA-RNA}^{Coulomb} + \Delta G_{DNA-RNA}^{van\ der\ Waals}$$

Coulomb interactions between the phosphate groups of the backbone and the other ions in the solution

van der Waals interactions between the rings on the two sides of the duplex.

$$\Delta G_{single\ strand}^{solvent} = \Delta G_{DNA}^{solvent} + \Delta G_{RNA}^{solvent}$$

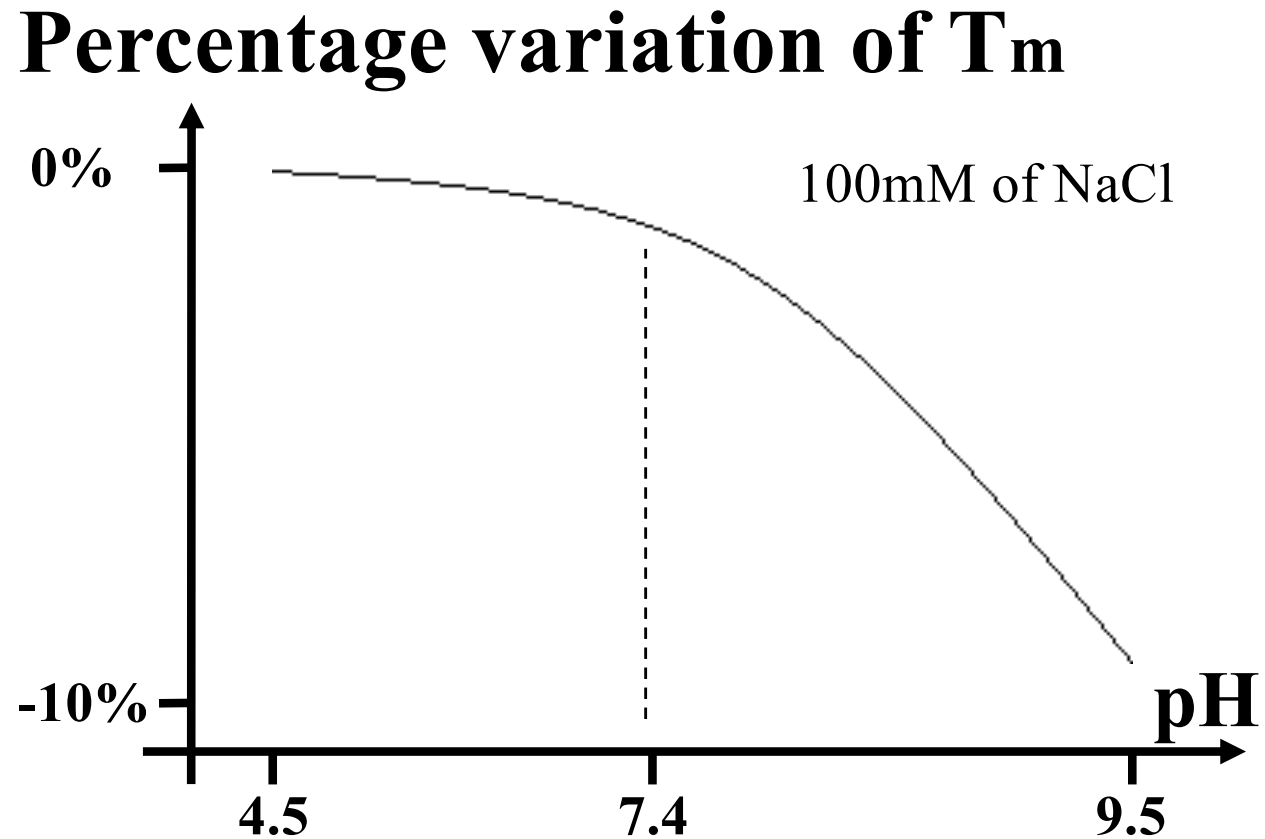
interactions between the different single strands and the solvent

DNA Denaturation

Melting of the DNA helix is the thermodynamic process that unwind the double helix and interrupts the non-covalent and sequence-dependent interactions between two single strands. The denaturation of DNA is another name for the same process.

The term **melting** is usually accomplished by heating the solutions containing the DNA. We can then follow the process by the **Melting Temperature**, and also have here another proof of the role of the solvent

Melting temperature changes by pH



Dependence by other solution ions

$$T_m = \frac{\Delta H}{\Delta S - R \ln C_{DNA}}$$

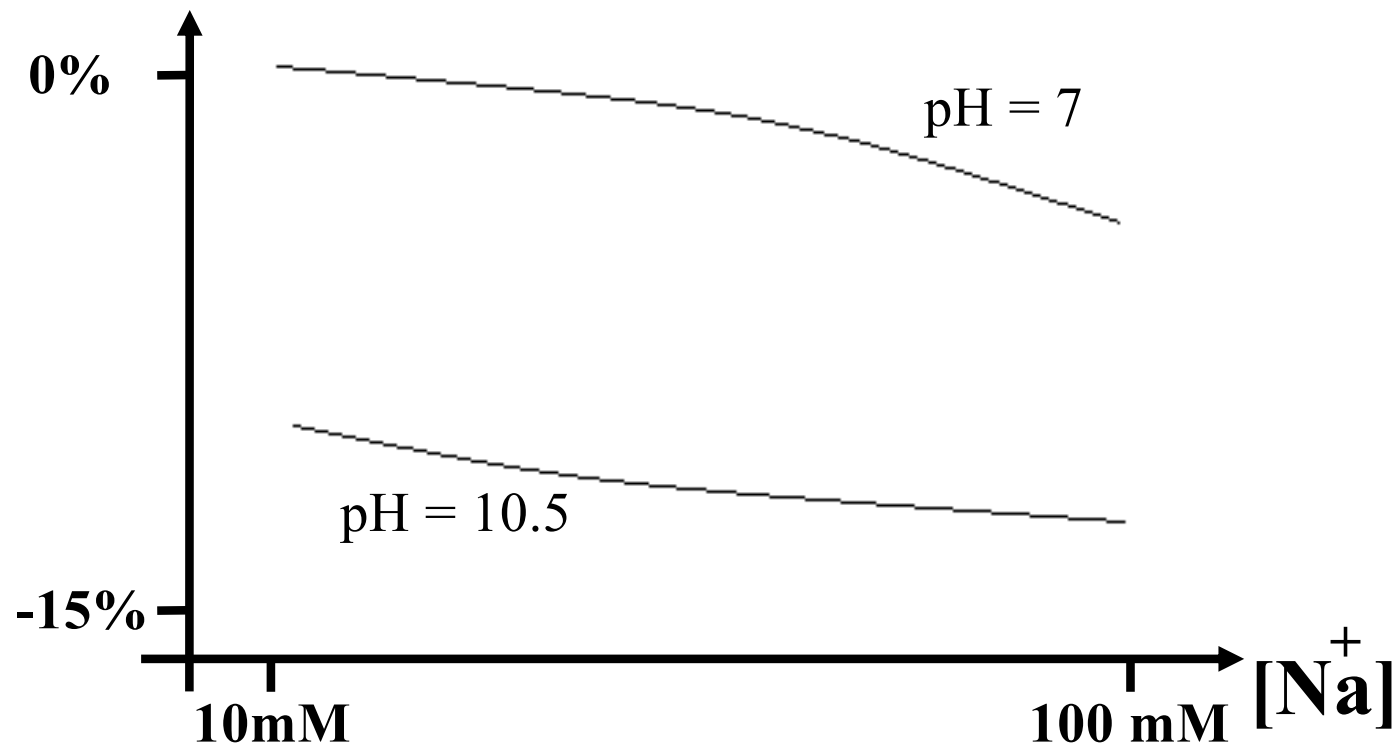
The enthalpy is usually considered independent of ions concentration, while Gibbs free energy and entropy are not.

$$\begin{cases} \Delta G_{37^\circ}^{[Na^+]} = \Delta G_{37^\circ}^{[1 \text{ Mole of } Na^+]} + \alpha N \ln[Na^+] \\ \Delta S_{37^\circ}^{[Na^+]} = \Delta S_{37^\circ}^{[1 \text{ Mole of } Na^+]} + \beta N \ln[Na^+] \end{cases} \quad \begin{cases} \alpha = -0.114 \\ \beta = +0.368 \end{cases}$$

The pH also affects the hydrogen bonds strength by changing the value of the Gibbs free energy of the interactions between single or double strands and the solvent

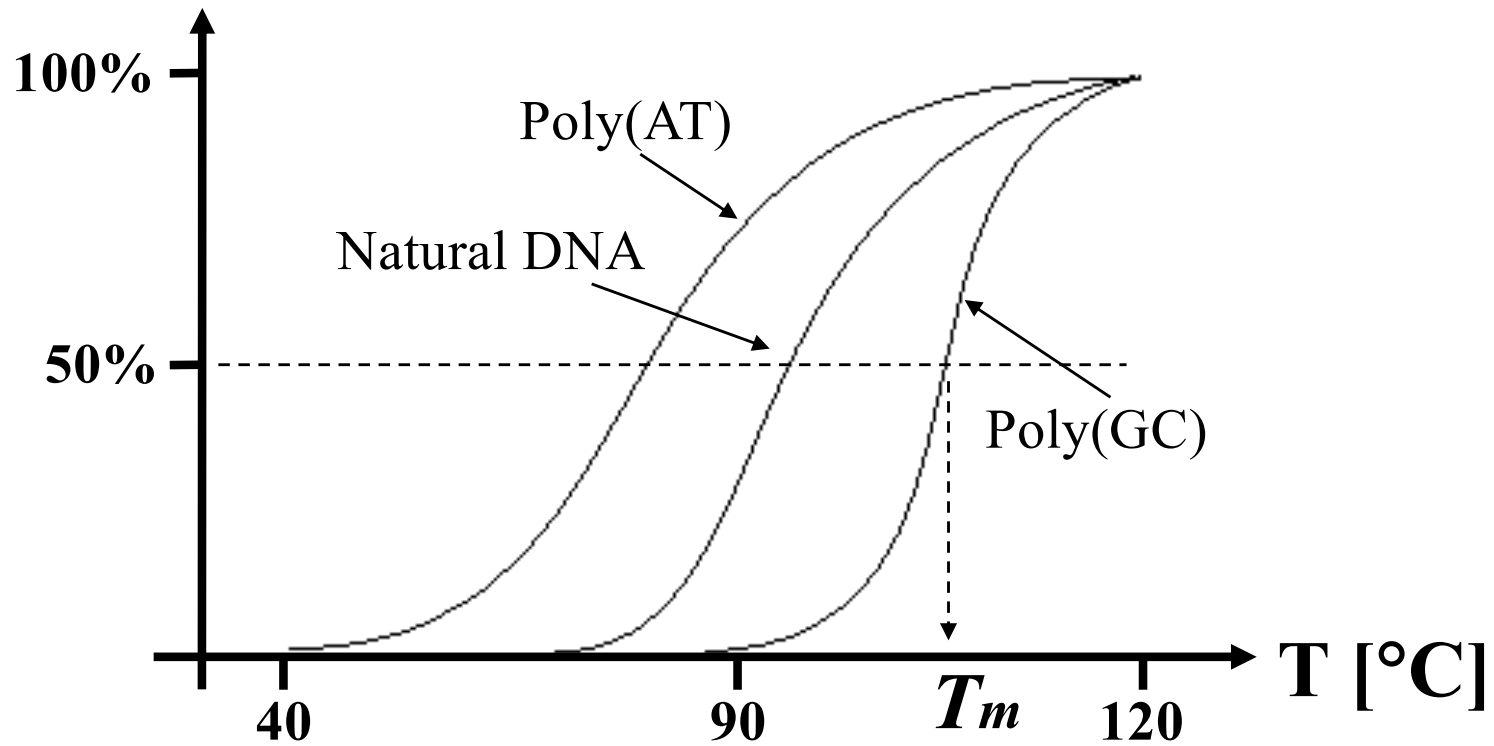
Melting temperature of DNA versus sodium concentration

Percentage variation of T_m



Melting processes for different DNA sequences

Percentage of double helix



NN-model versus Measurements

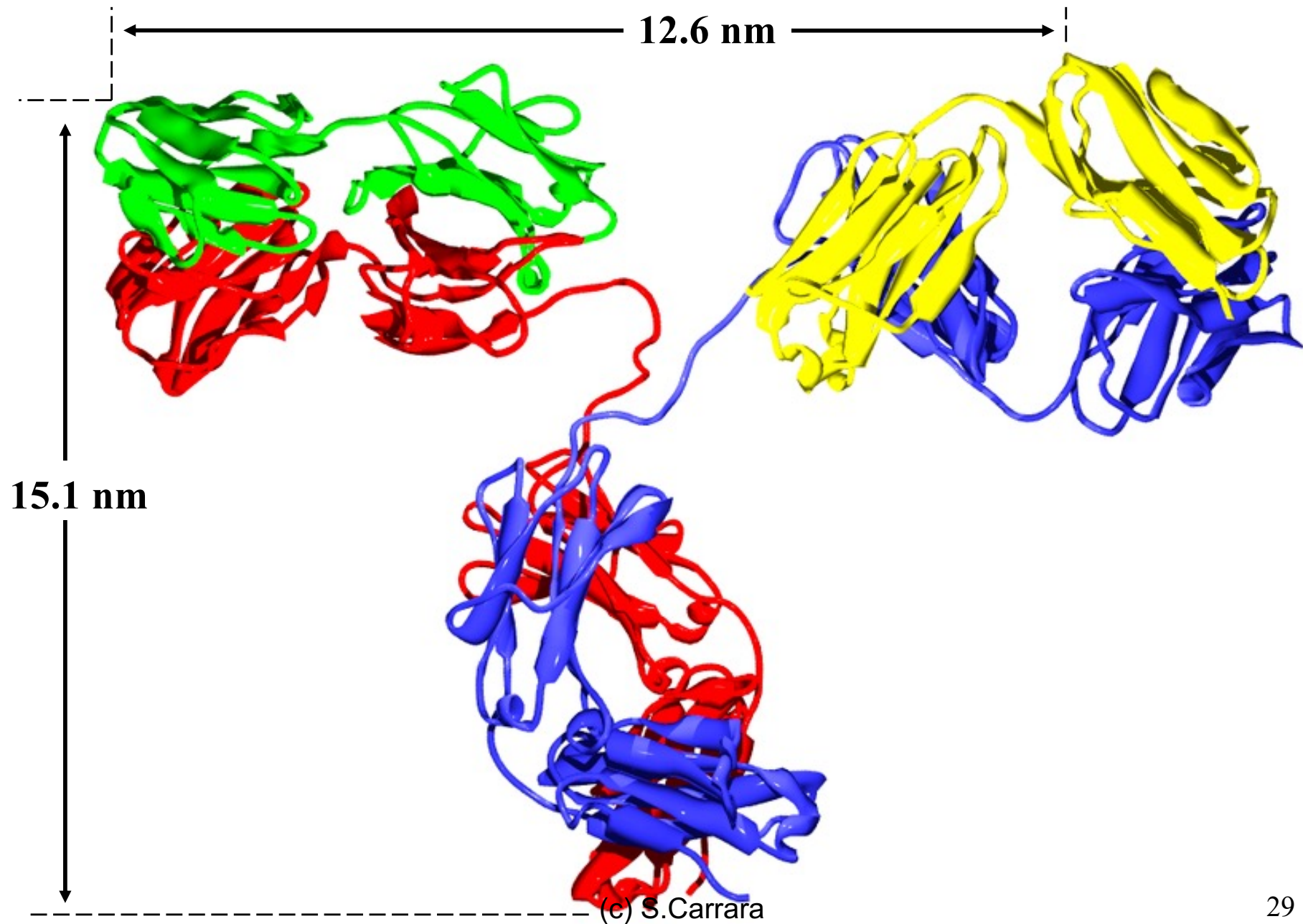
duplex	<i>NN-model</i> ΔG [kJ/mol]	<i>Experimental</i> ΔG [kJ/mol]
GGTTATTGG CCAATAACC	-25.4	-26.8
GGTTCTTGG CCAAGAACC	-30.1	-31.4
GGTTTTTGG CCAAAAACC	-27.6	-29.5
GGTTATTGG CCAA A AACC	-13.8	-12.0
GGTT C TTGG CCAATAACC	-12.1	-12.4
GGTTTTTGG CCAAG A AACC	-17.5 (c) S.Carrara	-17.5

Antibody/Antigen interactions

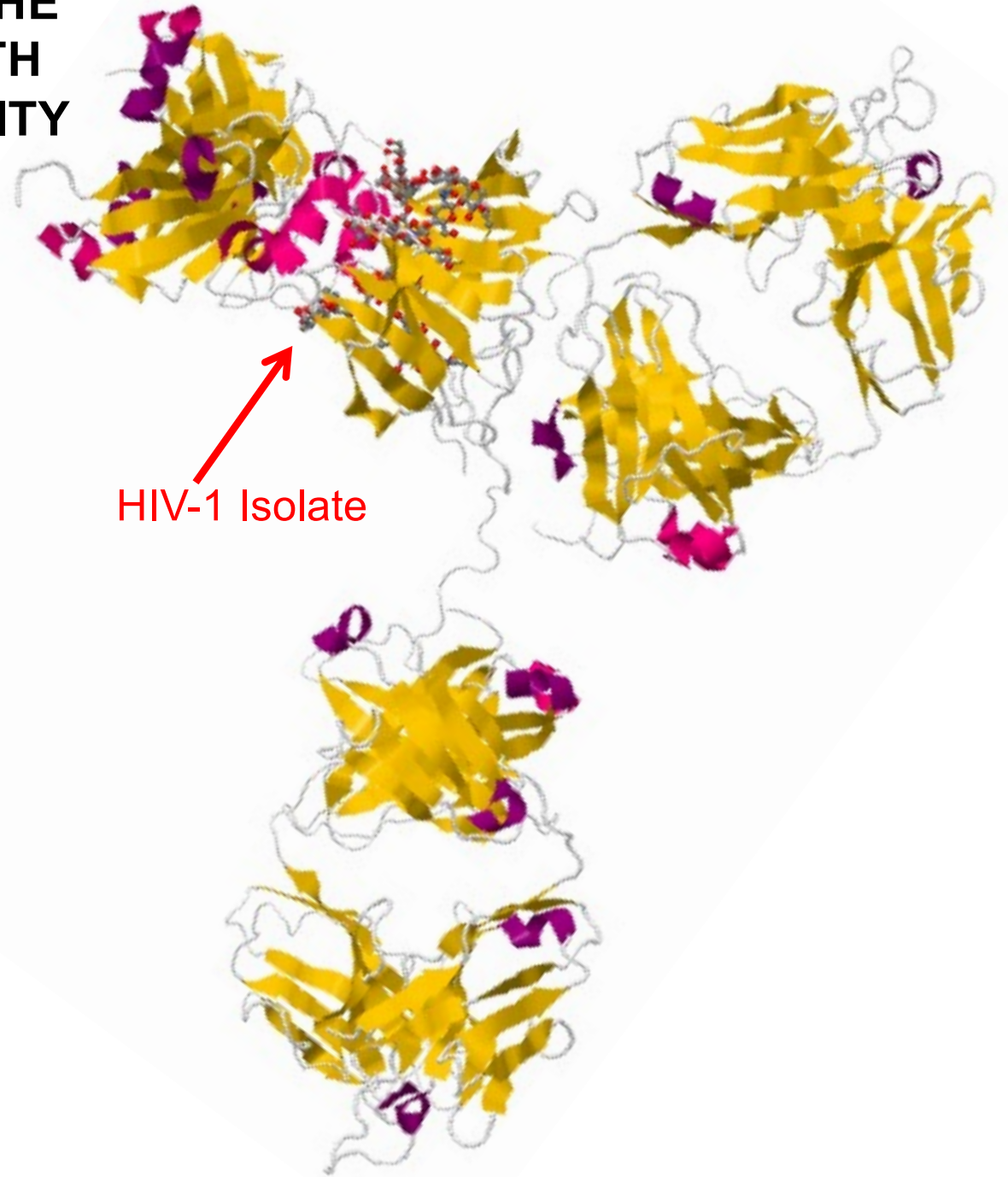
Antibodies are a large class of y-shaped proteins called immunoglobulins. An antibody shows a Y-structure with three main protein regions: a constant region and two variable regions. The variable regions are suitable for blocking the antigens. The protein blocks the antigen by closing the b-sheets in the variable region like fingers of a human hand when grasping

An efficient trapping is assured by the perfect match between the steric shape of the antigen and the 3D conformation of the antibody. The right part of the antigen in direct contact with the antibody is called the **epitope**, while the right part of the antibody in contact with the antigen is called the **paratope**

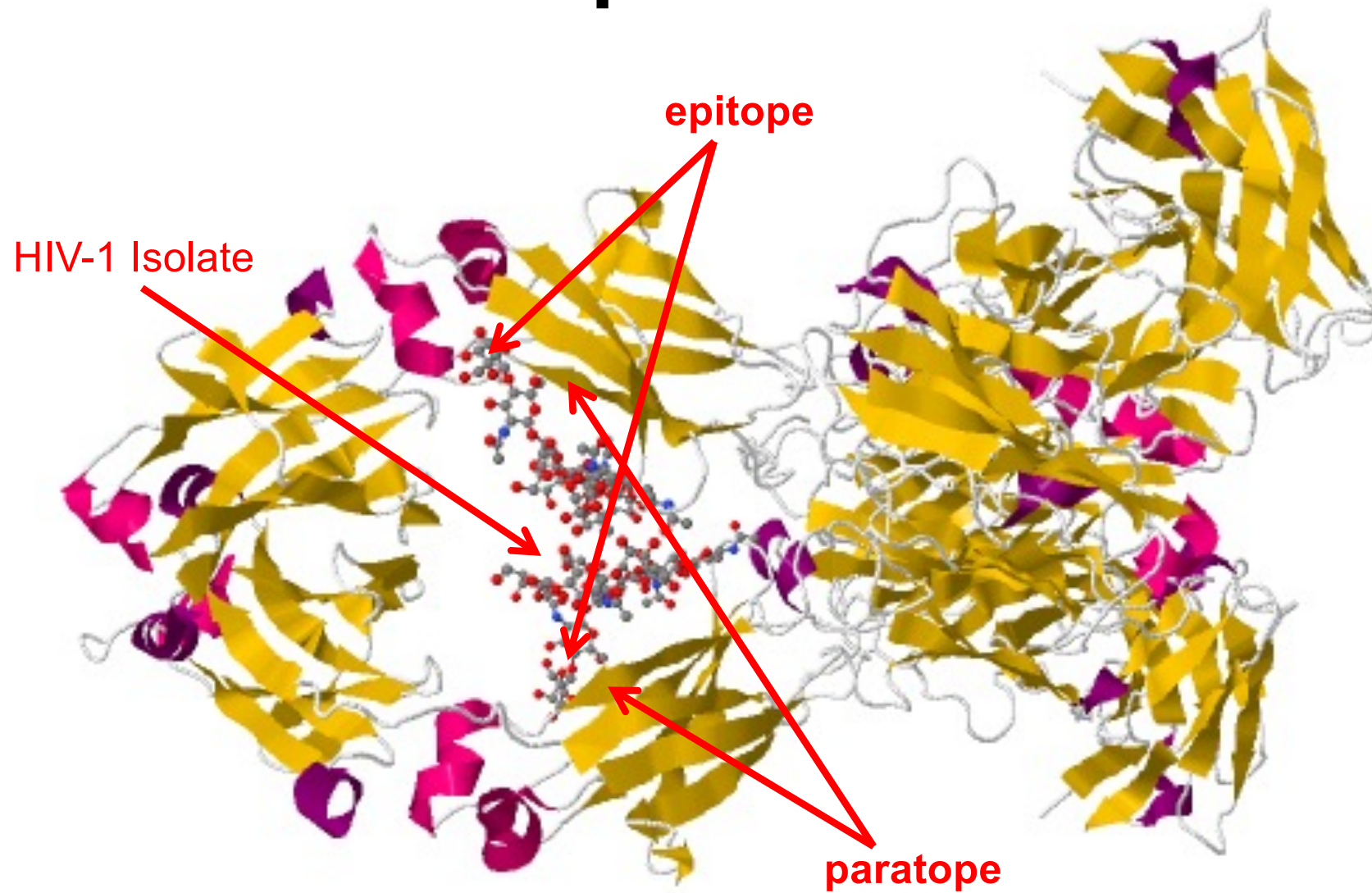
Antibody



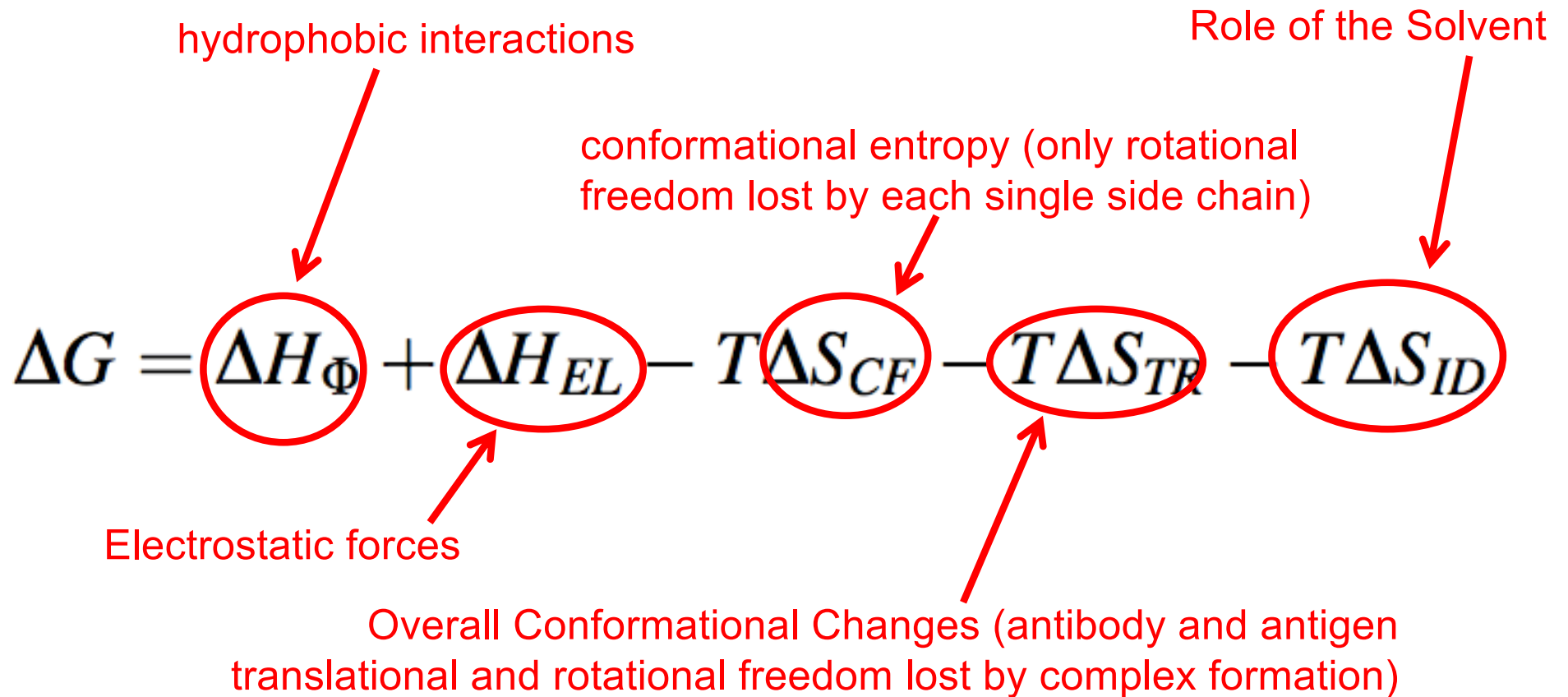
**CRYSTAL STRUCTURE OF THE
INTACT HUMAN IGG B12 WITH
BROAD AND POTENT ACTIVITY
AGAINST PRIMARY HIV-1
ISOLATES**



Top View



Gibbs free energy contributions



The diagram shows the equation $\Delta G = \Delta H_{\Phi} + \Delta H_{EL} - T\Delta S_{CF} - T\Delta S_{TR} - T\Delta S_{ID}$ with five terms circled in red. Red arrows point from descriptive text to each circled term: 'hydrophobic interactions' to ΔH_{Φ} , 'Electrostatic forces' to ΔH_{EL} , 'conformational entropy (only rotational freedom lost by each single side chain)' to $T\Delta S_{CF}$, 'Overall Conformational Changes (antibody and antigen translational and rotational freedom lost by complex formation)' to $T\Delta S_{TR}$, and 'Role of the Solvent' to $T\Delta S_{ID}$.

$$\Delta G = \Delta H_{\Phi} + \Delta H_{EL} - T\Delta S_{CF} - T\Delta S_{TR} - T\Delta S_{ID}$$

hydrophobic interactions

conformational entropy (only rotational freedom lost by each single side chain)

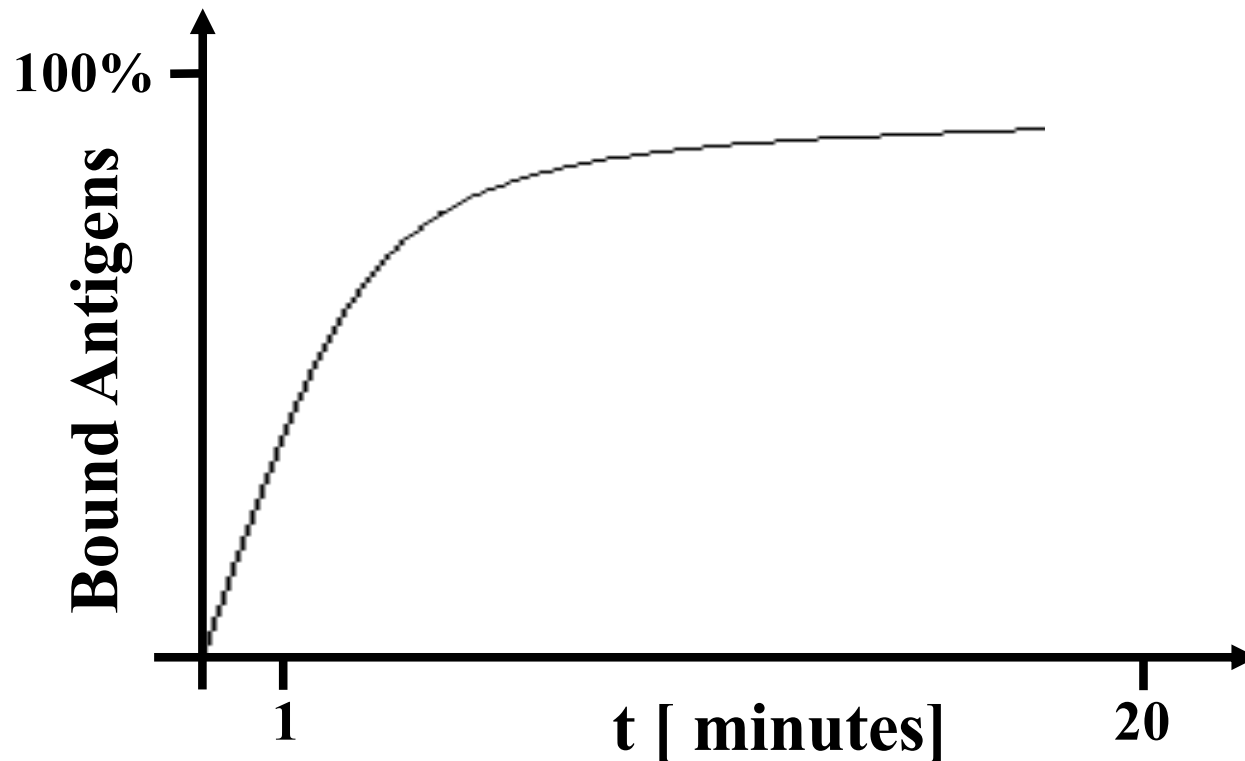
Role of the Solvent

Electrostatic forces

Overall Conformational Changes (antibody and antigen translational and rotational freedom lost by complex formation)

The total Gibbs free energy is related to various sources of molecular interactions

Typical trend of antigen binding versus time

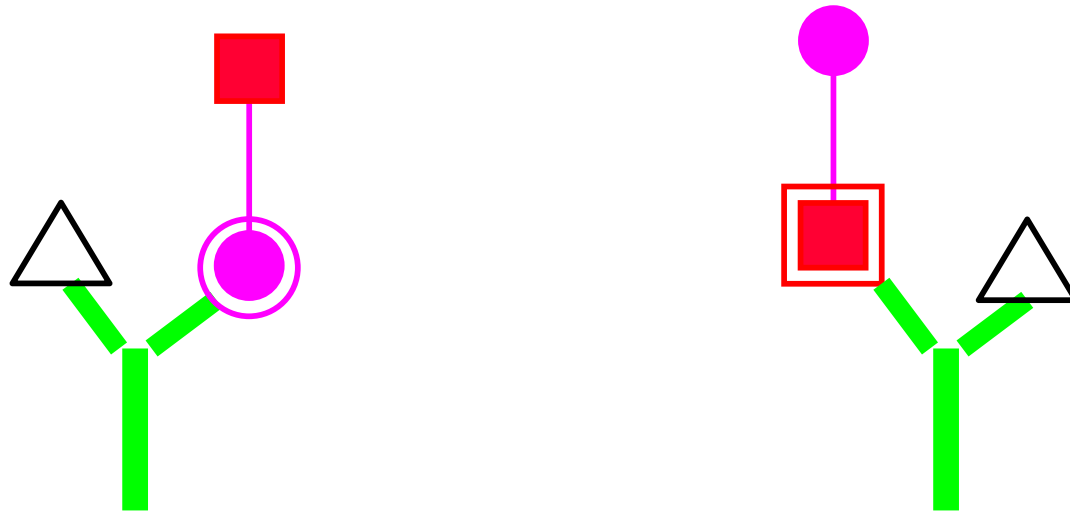


Different Kinds of Antibody

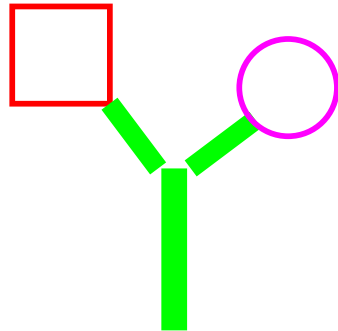
Dealing with real cases results in a bit more complex situation than just adding antigens to antibodies with a unique perfect match. Monoclonal antibodies are, then, all antibodies that have exactly the same specificity because they are from the same cloned single cell. However, antibodies are in general secreted in blood plasma by cells that are from different cell lines. Therefore, it is easy to obtain antibodies that are all against the same antigen but that do not have exactly the same specificity: these are polyclonal antibodies. Different kinds of antibodies means different kinetics on the same antigen.

We may also obtain different kinetics by involving the same antibody. It happens when the secreted antibody possesses two different paratopes to address two different epitopes of the same antigen

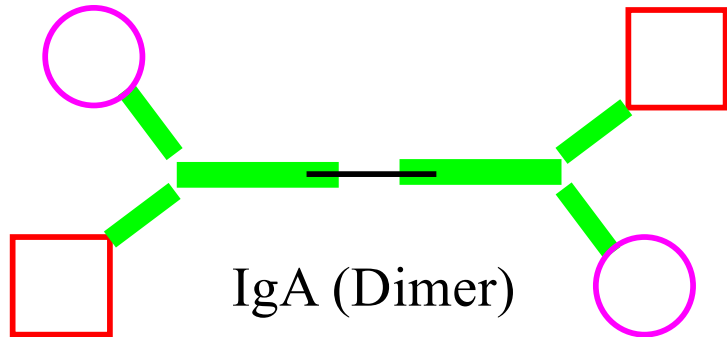
Polyclonal Antibodies to the same Antigen



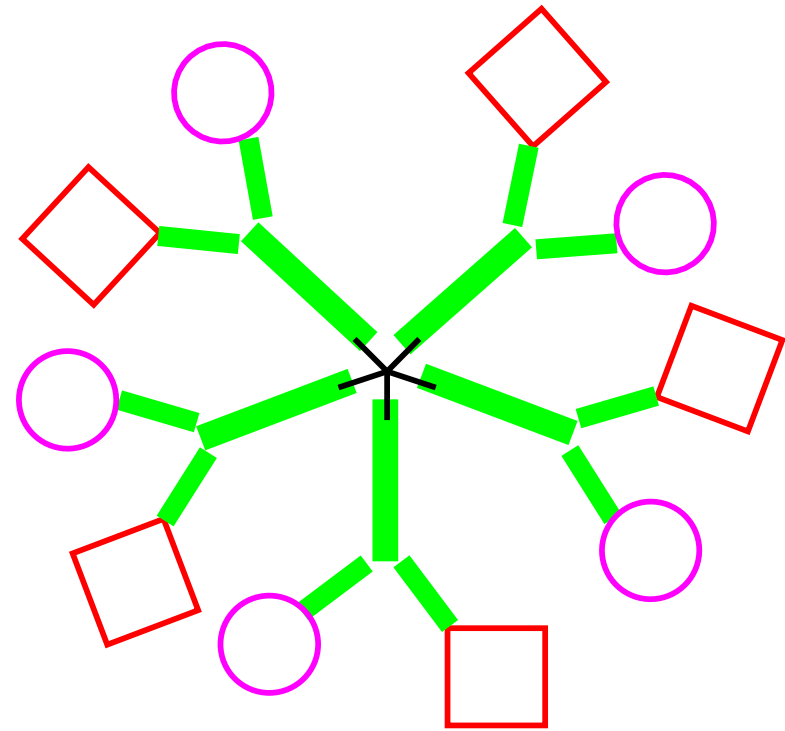
Classes of Immunoglobulins



IgG, IgE, and IgD (Monomer)



IgA (Dimer)



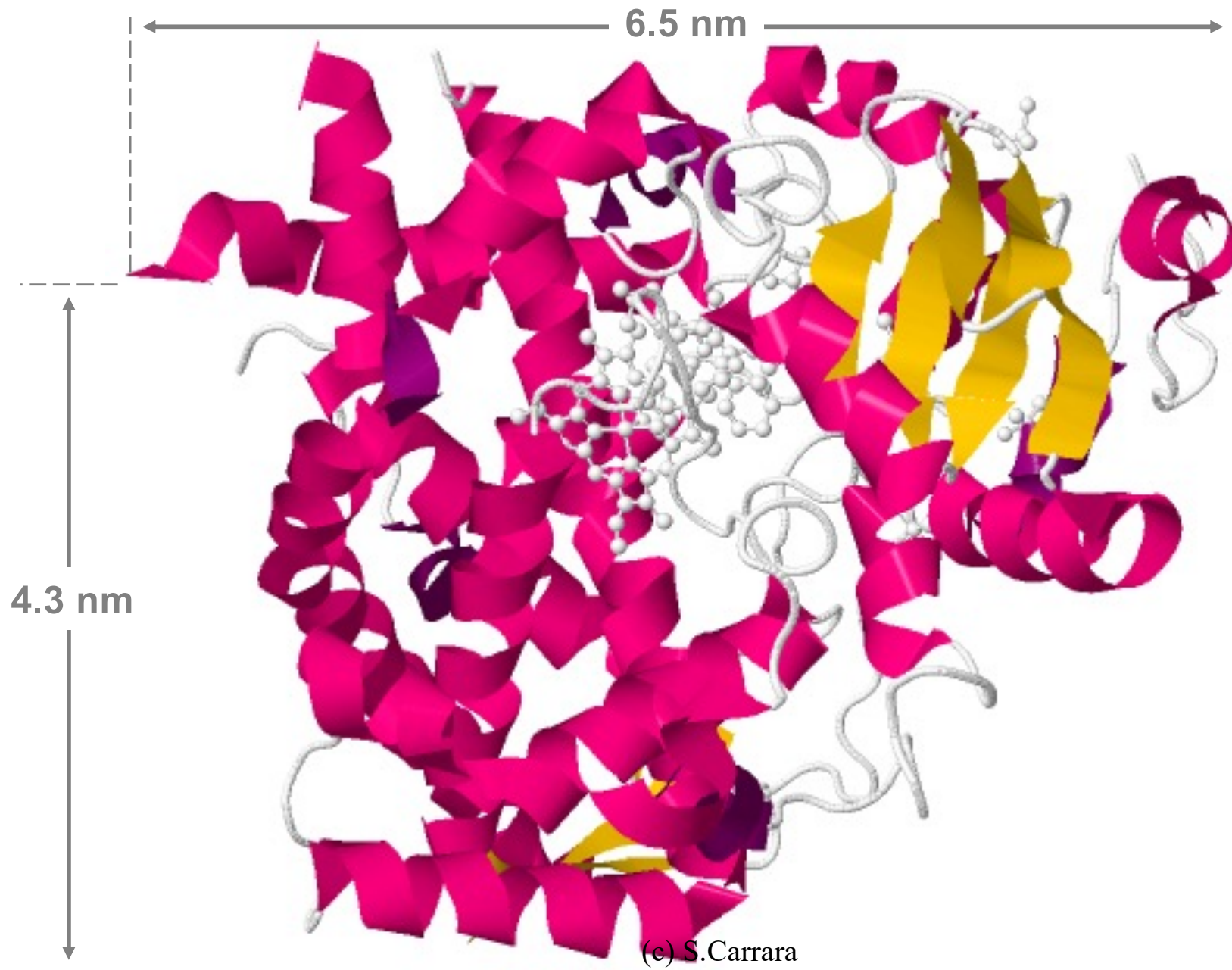
IgM (Pentamer)

Enzyme/Substrate interactions

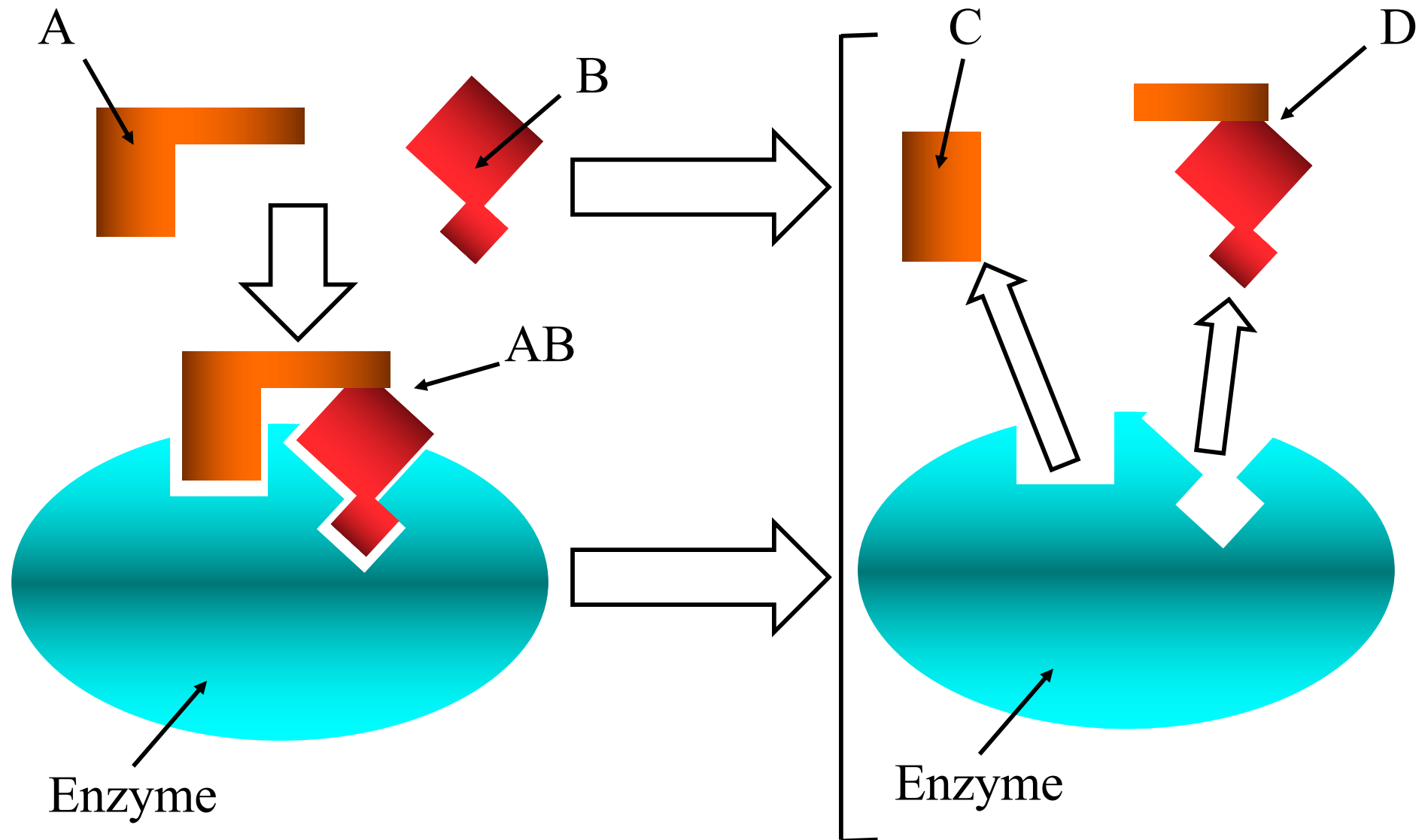
Enzymes are highly selective catalysts, accelerating both the rate and specificity of metabolic reactions. Almost all chemical reactions in a biological cell need enzymes in order to occur at a sufficient rates compatible with life. Most enzymes are proteins, although some catalytic RNA molecules have been identified.

At the beginning of an enzymatic reactions, is called **substrates** the molecules which transformation is catalysed. This molecules are converted into different ones, called **products**.

Cytochromes P450



Mechanism of Enzymatic reactions




Enzymatic Process

$$K = \frac{k_F}{k_B} = \frac{[C][D]}{[A][B]}$$

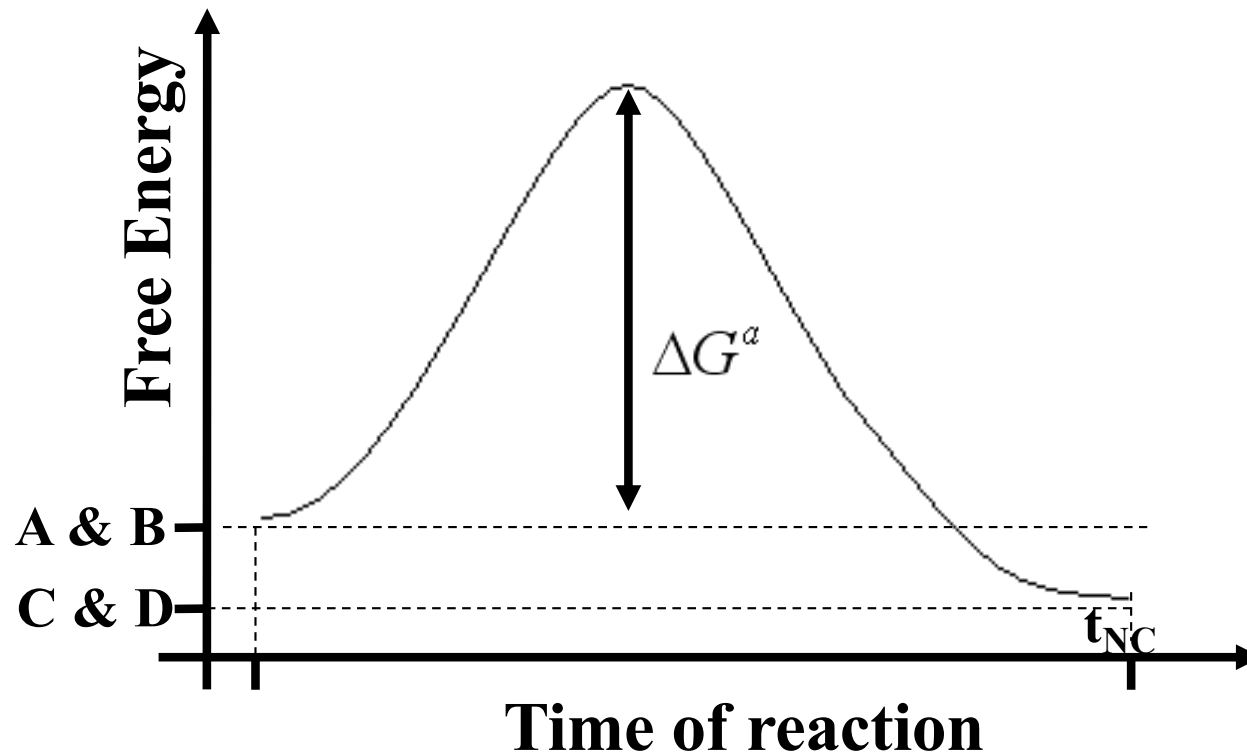
It is worth noting that the presence of an enzyme changes neither the equilibrium constant nor the two forward and backward rates

The enzyme changes the timing of the chemical reaction. If the equilibrium is reached in, let say, 1 h in the absence of enzymes, then it might be reached in few seconds in the presence of the suitable enzyme!

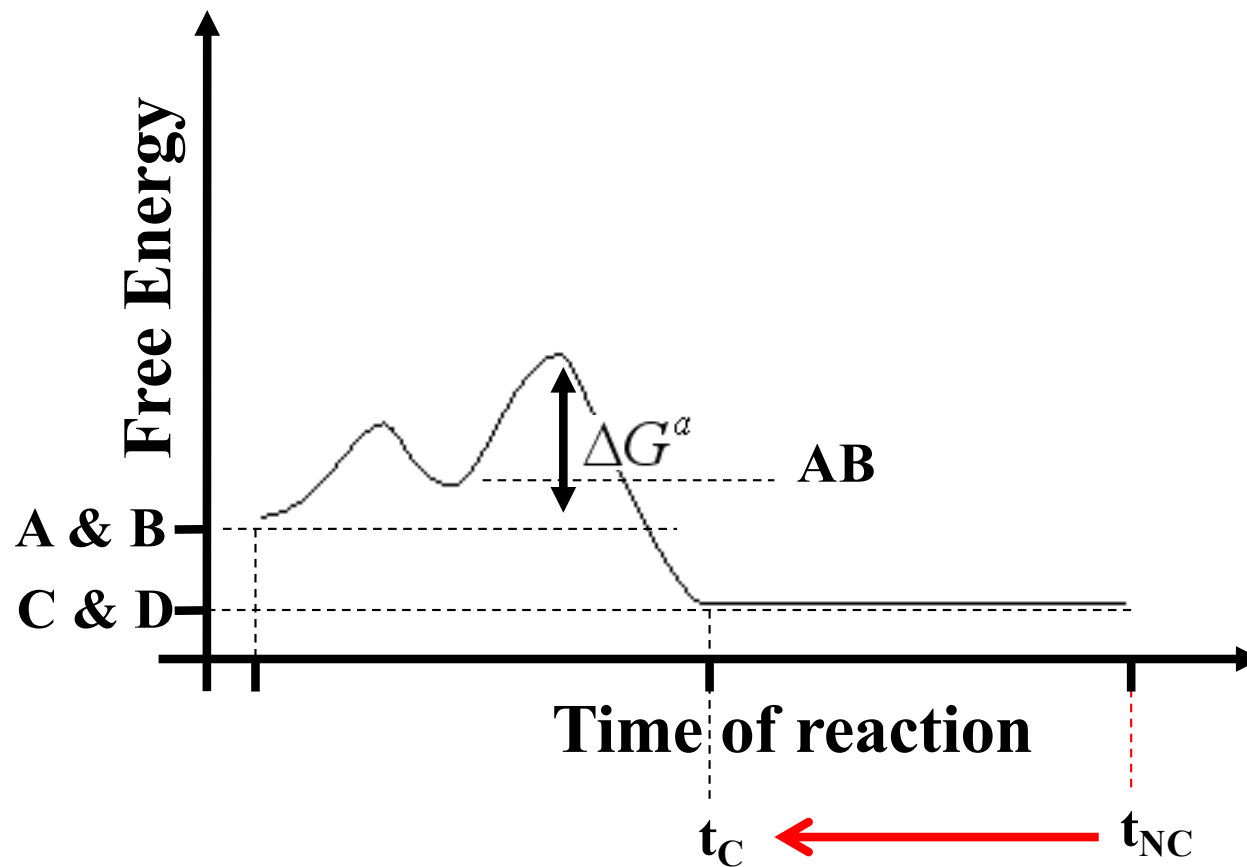
Gibbs free energy

$$\frac{d([C][D])}{dt} = k_p[AB] = k_p[A][B] e^{-\frac{\Delta G^a}{RT}}$$


Free energy of a reaction without enzymes

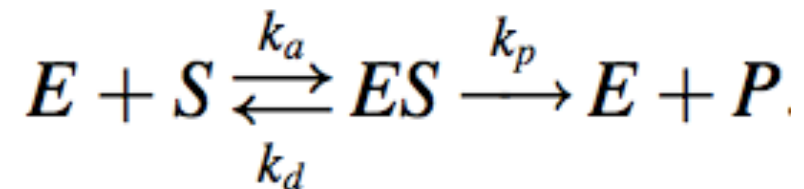


Free energy of a reaction with enzymes



Michaelis-Menten Kinetics

More often, the compound B is a common molecule, such as oxygen, or water, or proton, that is not specific to the enzyme action. Therefore, the enzymatic process is re-written in a form that explicitly introduce the presence of the enzyme:



By neglecting the possibility for E and P to give back the intermediate state AB, we can now write the net rate of product formation as:

$$\frac{d[P]}{dt} = k_p[ES]$$

Michaelis-Menten Kinetics

While the rate of complex formation:

$$\frac{d[ES]}{dt} = k_a[E][S]$$

And the rate of complex breakdown:

$$\frac{d([E][S])}{dt} + \frac{d[P]}{dt} = (k_d + k_p)[ES]$$

Need to be equal at the steady state of the enzymatic reaction:

$$k_a[E][S] = (k_d + k_p)[ES]$$

Michaelis-Menten Kinetics

Thus, the concentration of the complex is:

$$[ES] = \frac{k_a}{(k_d + k_p)} [E][S]$$

Which defines the so-called **Michaelis' constant**:

$$K_M = \left(\frac{k_a}{(k_d + k_p)} \right)^{-1}$$

The Michaelis constant is so important because it shows how efficient is the enzyme in forming the intermediate state that is required to catalyze the reaction.

Michaelis-Menten Kinetics

Usually, there is a certain amount of available enzymes that are still free to accept further substrates:

$$[E] = [E]_0 - [ES]$$

With $[E]_0$ as the initial concentration of total enzymes, which enables to re-write the concentration of the complex:

$$[ES] = \frac{([E]_0 - [ES])[S]}{K_M}$$

Or:

$$[ES] = [E]_0 \frac{[S]}{[S] + K_M}$$

Michaelis-Menten Kinetics

Now, by defining the reaction velocity V and the maximum reaction velocity V_m , respectively, as:

$$V = \frac{d[P]}{dt} \quad V_{\max} = k_p[E]_0$$

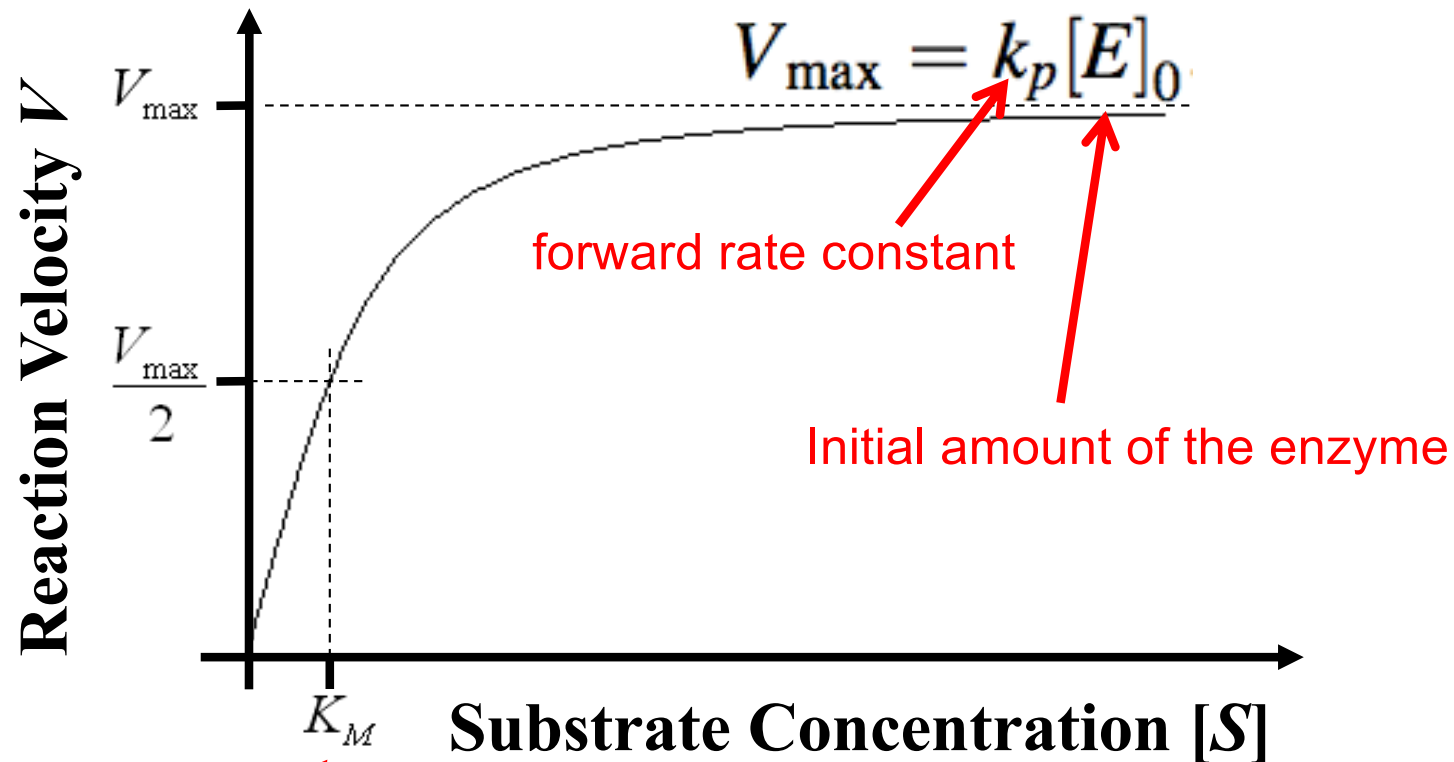
If we, then, go back to couple of previous equations:

$$\frac{d[P]}{dt} = k_p[ES] \quad [ES] = [E]_0 \frac{[S]}{[S] + K_M}$$

We can finally write the the so-called **Michaelis–Menten equation**:

$$V = V_{\max} \frac{[S]}{[S] + K_M}$$

Michaelis-Menten Kinetics



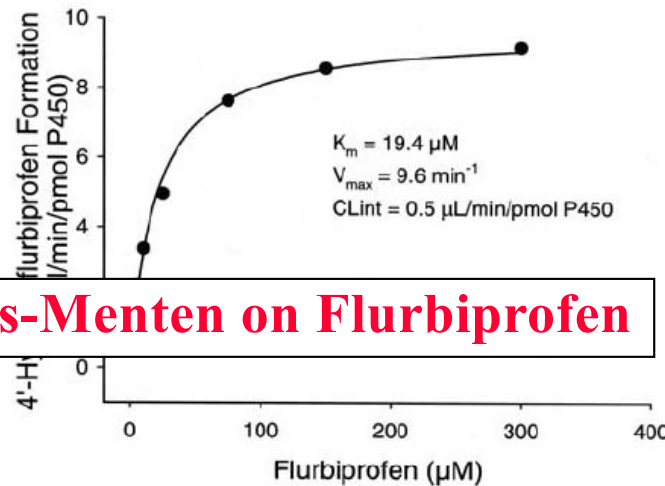
Depends only by the association and dissociation constants and by the forward rate

Atypical Enzymatic Reactions

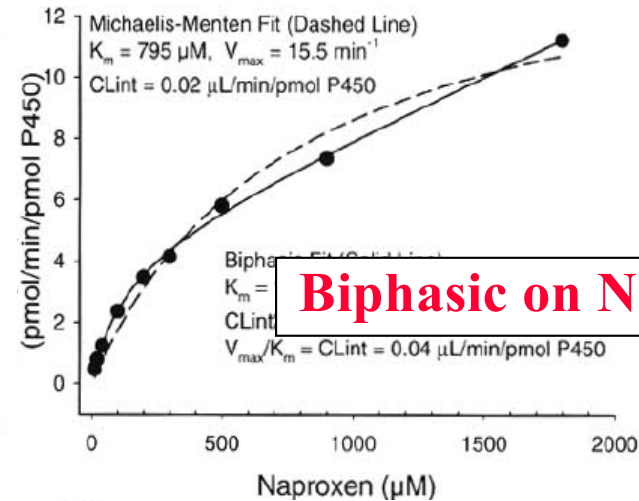
One example of enzymes that have more than one substrate and that present other kinetics than the Michaelis–Menten is the case of **Cytochromes P450**. They are key enzymes in the metabolism of any mammalian. These proteins catalyze the redox reaction of various compounds and, sometimes, show atypical kinetics.



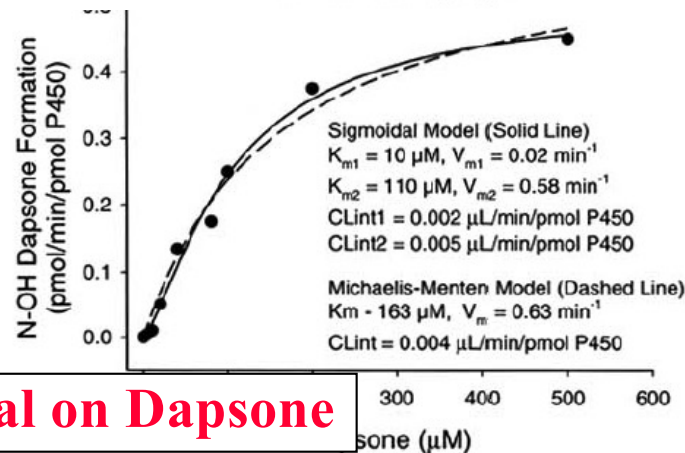
HOMOTROPIC KINETICS



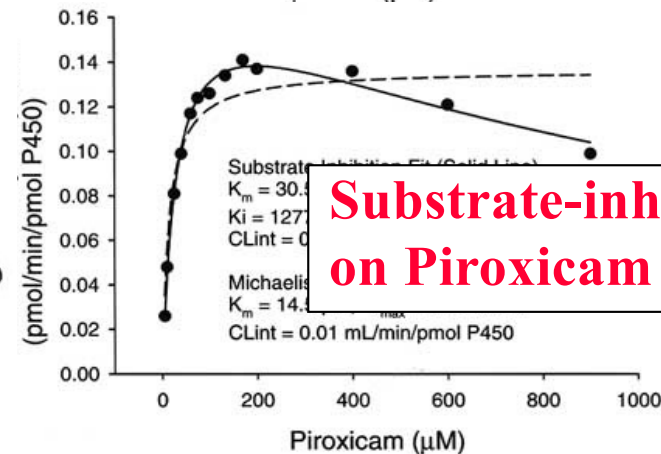
Michaelis-Menten on Flurbiprofen



Biphasic on Naproxen



Sigmoidal on Dapsone



Substrate-inhibition on Piroxicam

Timothy S. Tracy, *Current Drug Metabolism*, 2003, Vol. 4, No. 5

The isoform 2C9 of the cytochrome P450 presents all previously mentioned kinetics upon different substrates!

Phenomena of Heterotropic Kinetics

D1

- **HETERO ACTIVATION**

D2

The presence of D2 activates
The catalysis on D1

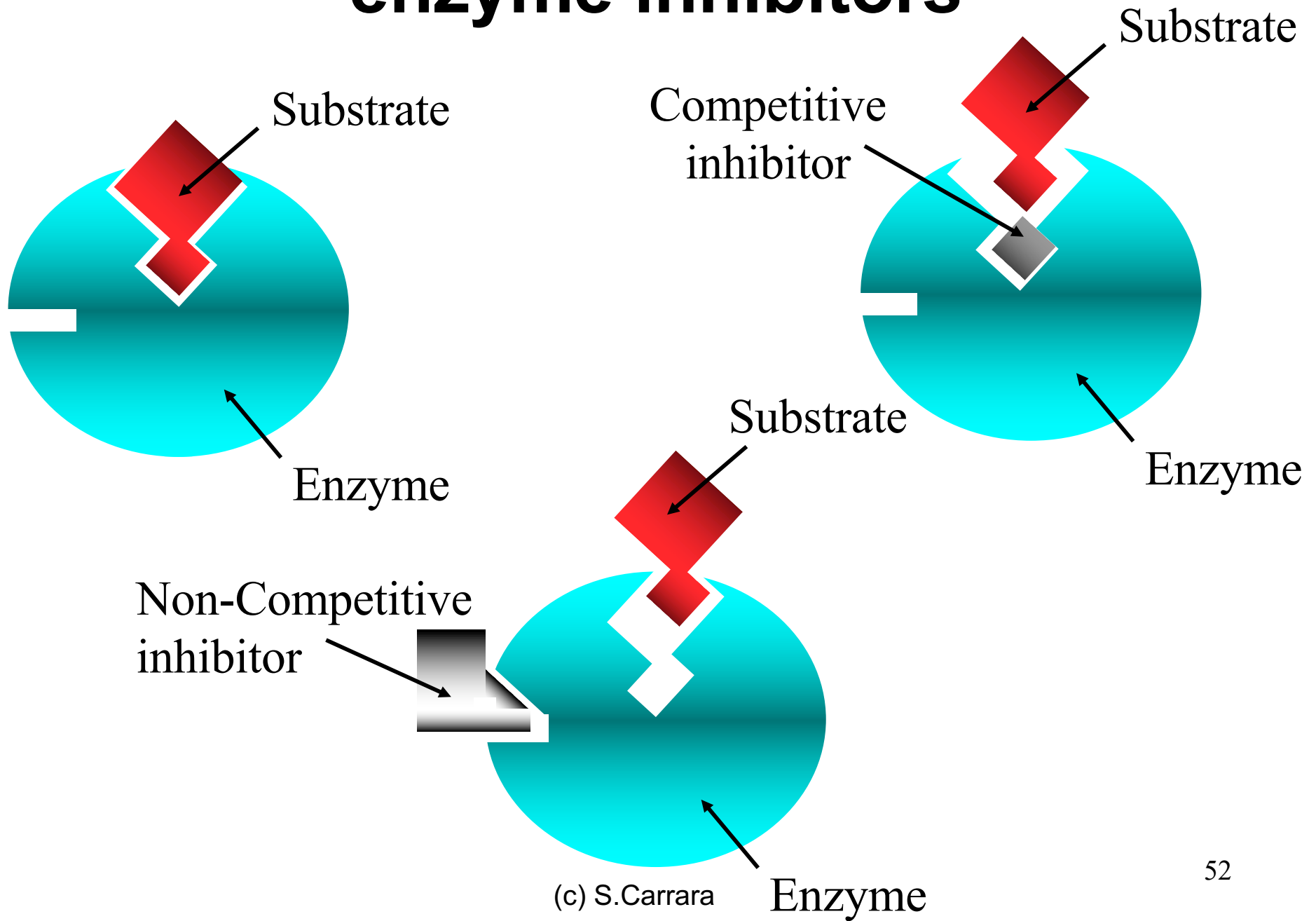
D1

- **PARTIAL INHIBITION**

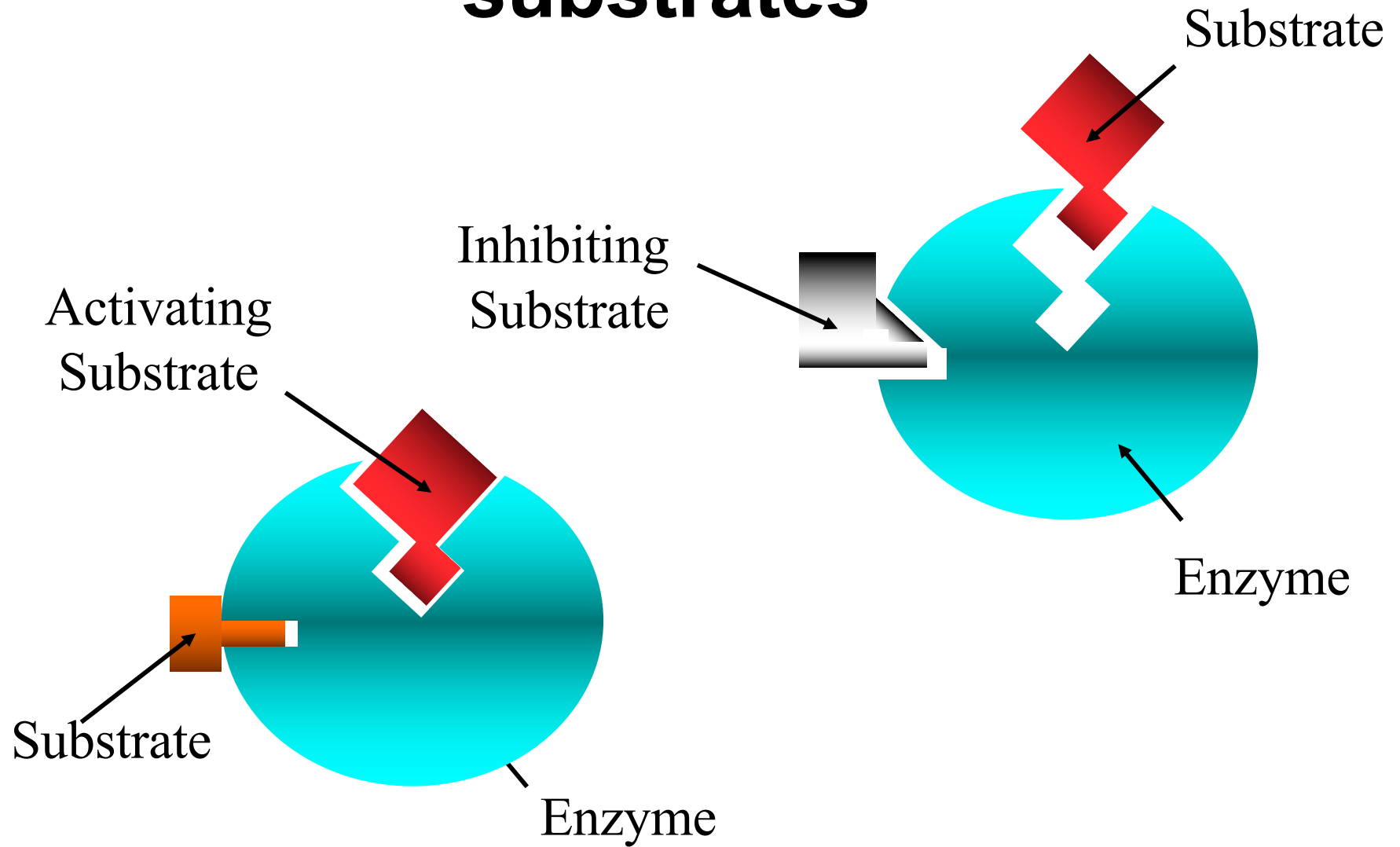
D2

The presence of D2 inhibits
The catalysis on D1

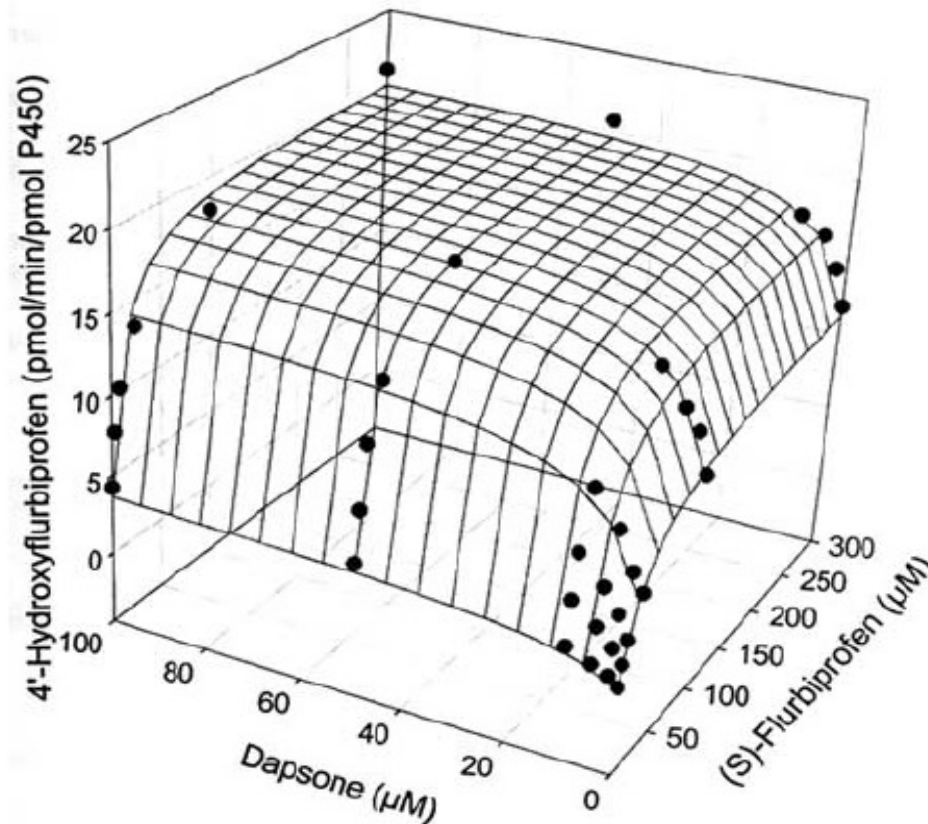
Competitive and noncompetitive enzyme inhibitors



Activating and inhibiting enzyme substrates



The case of Cytochrome P450 2C9



Timothy S. Tracy, *Current Drug Metabolism*, 2003, Vol. 4, No. 5

$$v = \frac{V_{\max}[S]}{k_m \left(\frac{1 + \frac{[E]}{K_s}}{1 + \frac{\epsilon'[E]}{\epsilon K_s}} \right) + [S] \left(\frac{1 + \frac{[E]}{\epsilon K_s}}{1 + \frac{\epsilon'[E]}{\epsilon K_s}} \right)}$$

B = effector (activator compound)

K_s = [B] producing half maximal effect

ϵ = change in K_m due to effector binding

ϵ' = change in V_{\max} due to effector binding

Heterotropic kinetics of flurbiprofen and dapsona
when catalysed by the enzyme P450 2C9